PHY 6646 - Quantum Mechanics II - Spring 2020 Homework set # 7, due February 26

1. A particle of mass μ is in linear motion in the potential

$$V(x) = 5kx \qquad \text{for } x > 0$$

= $-kx \qquad \text{for } x < 0 \qquad (0.1)$

with k positive. Use the WKB approximation to estimate the energies of the states of the particle.

2. Problems 16.2.7, 17.2.1, 17.2.2, 17.2.3 in Shankar's book.

3. Consider a particle of mass μ in the central force potential

$$V(r) = -\frac{e^2}{r} \qquad \text{for } 0 < r < R$$
$$= -\frac{e^2}{r} \exp\left(-\lambda(r-R)\right) \quad \text{for } R < r < \infty \quad . \tag{0.2}$$

This potential differs from the Coulomb potential only in the region r > R, where the Coulomb force is screened. The difference becomes negligible when $\lambda \to 0$. Consider this difference as a perturbation and calculate the first-order correction to the energy of the ground state of the hydrogen atom.