PHY 6645 - Quantum Mechanics I - Fall 2018 Homework set # 2, due September 5

- 1. Problems 1.9.1, 1.9.2, 1.9.3, 1.10.1, 1.10.2, 1.10.3 and 1.10.4 in Shankar's book.
- 2. Show that

$$e^{\Omega} \equiv \sum_{p=0}^{\infty} \frac{1}{p!} \Omega^p = \lim_{n \to \infty} \left(1 + \frac{1}{n} \Omega \right)^n \tag{0.1}$$

where Ω is a linear operator.

3. Show that if U is a linear operator on a vector space \mathcal{V} and if for all vectors $V \in \mathcal{V}$

$$\langle V'|V'\rangle = \langle V|V\rangle \tag{0.2}$$

where |V'>=U|V>, then U must be a unitary operator on \mathcal{V} .