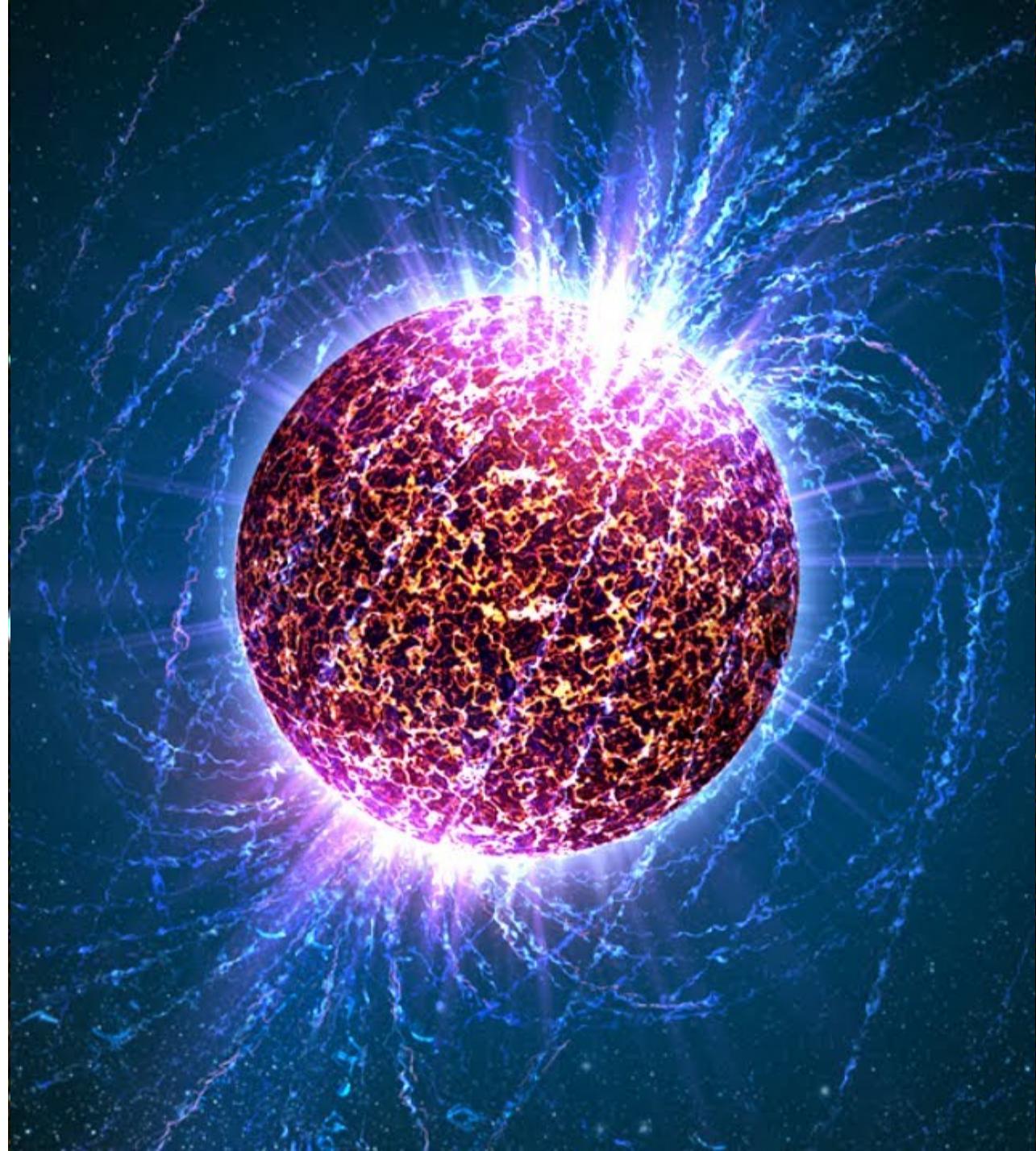


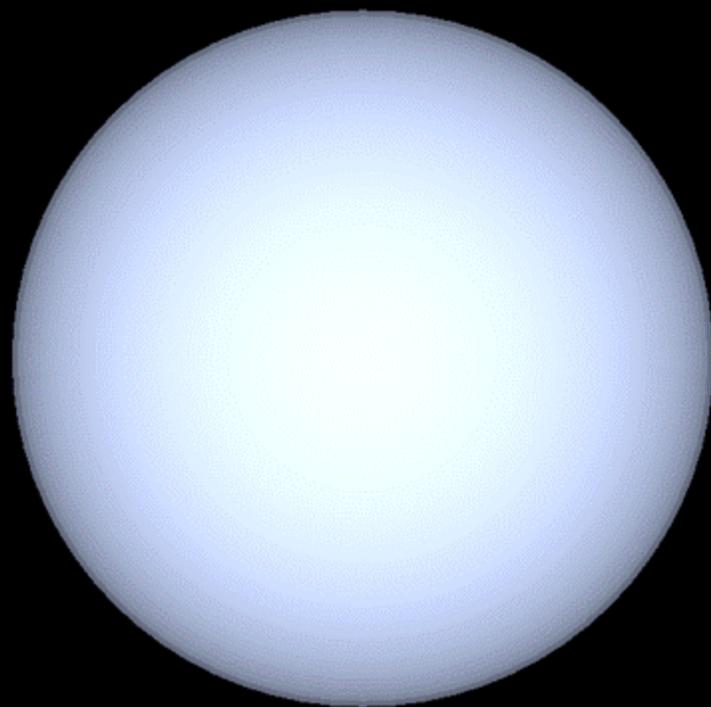
Lecture VI.

Neutron stars



Imre Bartos | Fall 2019

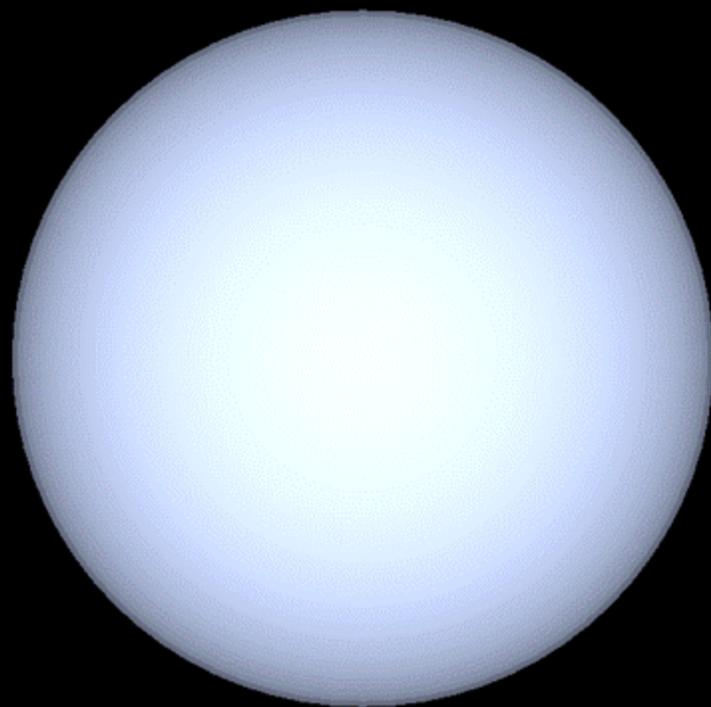




$$M \approx 1.0 M_{\text{sun}}$$

$$R \approx 5800 \text{ km}$$

$$V_{\text{esc}} \approx 0.02c$$



$$T = 2\pi \sqrt{\frac{a^3}{G(M_1 + M_2)}}$$

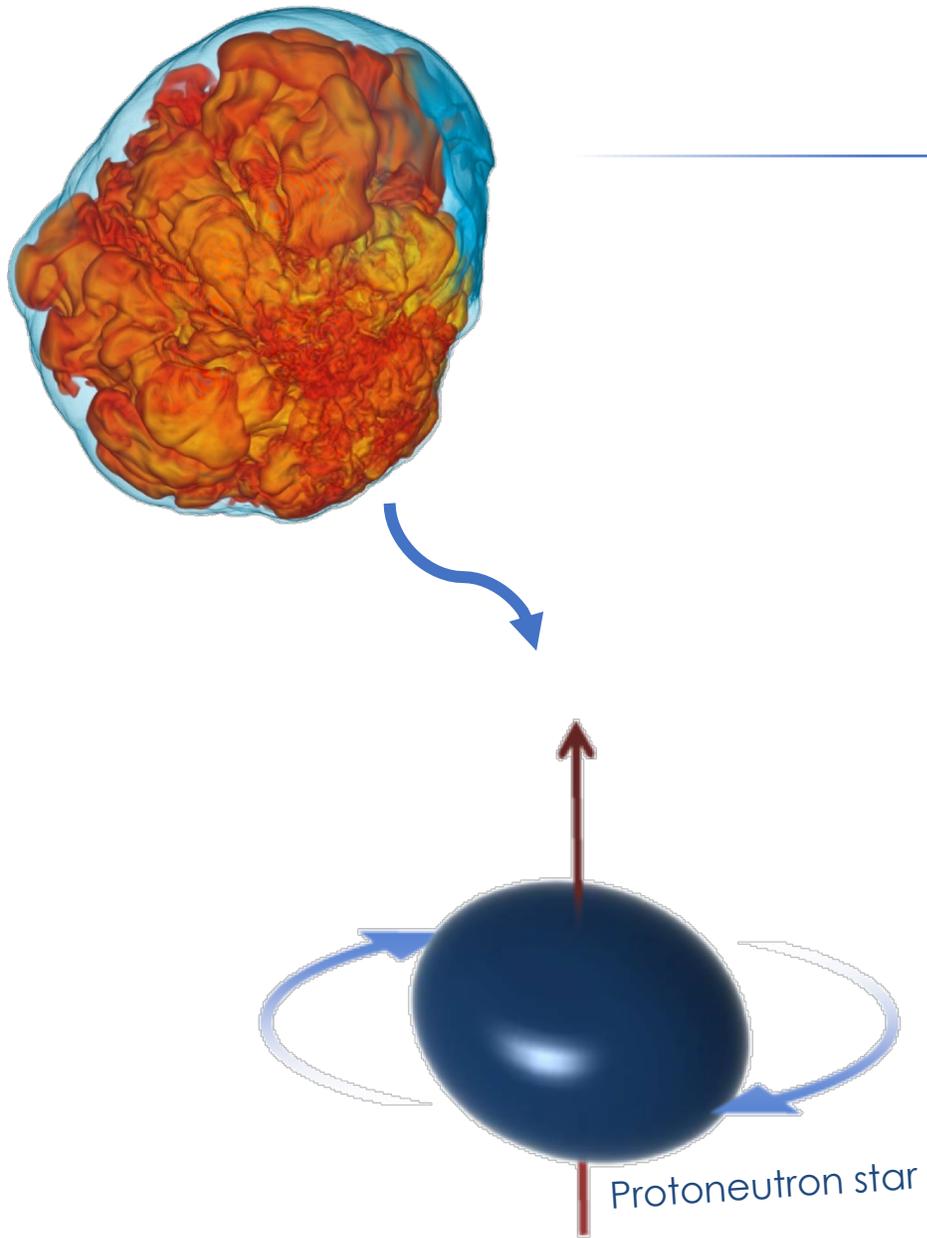
$M \approx 1.0 M_{\text{sun}}$
 $R \approx 5800 \text{ km}$
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Gravitational wave production

Process	Typical $ h $ (at 10 kpc)	Typical f (Hz)	Duration Δt (ms)	E_{GW} ($10^{-10} M_{\odot} c^2$)	Limiting Factors or Processes
Prompt Convection	$10^{-23} - 10^{-21}$ (Emission characteristics depend on seed perturbations.)	50 – 1000	0 – \sim 30	$\lesssim 0.01 - 10$	Seed perturbations, entropy/lepton gradient, rotation
PNS Convection	$2 - 5 \times 10^{-23}$	300 – 1500	500 – several 1000	$\lesssim 1.3(\frac{\Delta t}{1s})$	rotation, BH formation, strong PNS g -modes
Neutrino- driven Convection and SASI	$10^{-23} - 10^{-22}$ (peaks up to 10^{-21})	100 – 800	100 – \gtrsim 1000	$\gtrsim 0.01(\frac{\Delta t}{100ms})$ $\lesssim 15(\frac{\Delta t}{100ms})$	rotation, explosion, BH formation

Unclear, but likely only detectable from the Milky Way

Rapidly rotating core



GWs from rapidly rotating cores?

Relevant distance scale:

Low-luminosity GRB / CCSN with jets: $10^2\text{-}10^3 \text{ Gpc}^{-3} \text{ yr}^{-1}$
(Guetta & della Valle 2006; Soderberg+ Nature 2010)

(Beaming factor ~ 10)

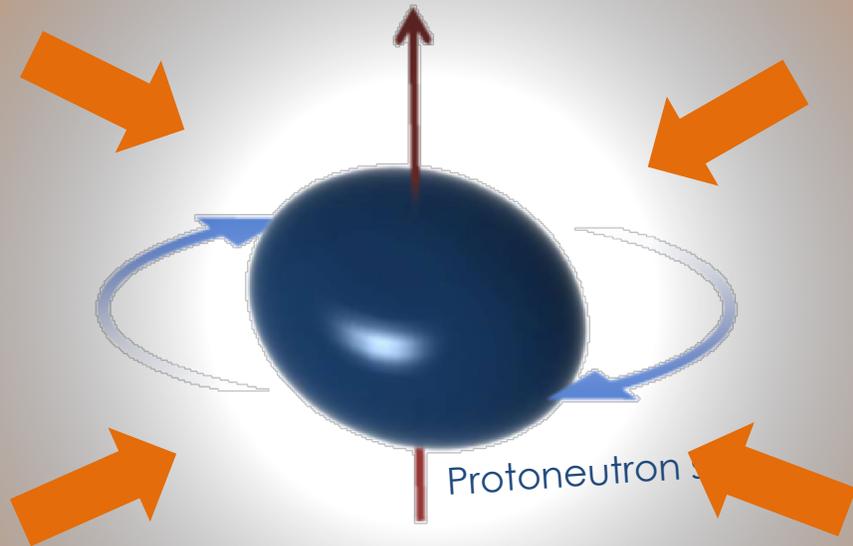
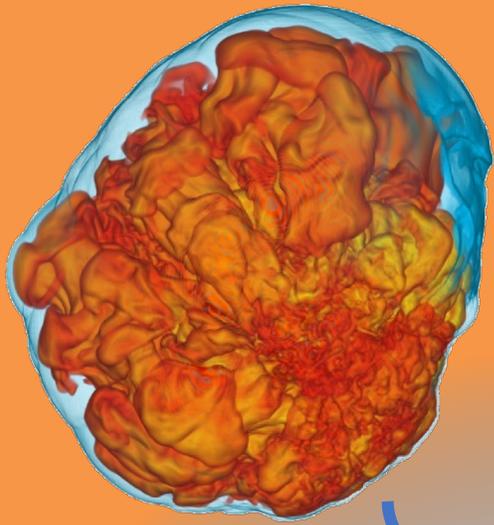
→ 50-100 Mpc

Differential rotation (e.g. Corvino+ 2010)

- **Dynamical instabilities** (*shorter time scale*)
- **Secular instabilities** (*longer time scale*)
- **Magnetic distortion**

$$E_{\text{GW}} \approx 10^{-2} M_{\odot} c^2 \left(\frac{\epsilon}{0.2} \right)^2 \left(\frac{f}{2 \text{ kHz}} \right)^6 \left(\frac{M}{1.4 M_{\odot}} \right) \left(\frac{R}{12 \text{ km}} \right)^2 \left(\frac{\tau}{0.1 \text{ s}} \right)$$

Rapidly rotating core



GWs from rapidly rotating cores?

Relevant distance scale:

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(Beaming factor ~ 10)

→ 50-100 Mpc

Differential rotation (e.g. Corvino+ 2010)

- **Dynamical instabilities** (*shorter time scale*)
- **Secular instabilities** (*longer time scale*)
- **Magnetic distortion**

Fallback accretion? (Piro, Thrane, 2012)

$$E_{\text{CW}} \approx 10^{-2} M_{\odot} c^2 \left(\frac{\epsilon}{0.2} \right)^2 \left(\frac{f}{2 \text{ kHz}} \right)^6 \left(\frac{M}{1.4 M_{\odot}} \right) \left(\frac{R}{12 \text{ km}} \right)^2 \left(\frac{\tau}{0.1 \text{ s}} \right)$$

Homework

$$E_{\text{GW}} \approx 10^{-2} M_{\odot} c^2 \left(\frac{\epsilon}{0.2} \right)^2 \left(\frac{f}{2 \text{ kHz}} \right)^6 \left(\frac{M}{1.4 M_{\odot}} \right) \left(\frac{R}{12 \text{ km}} \right)^2 \left(\frac{\tau}{0.1 \text{ s}} \right)$$

Assume realistic dependence of epsilon on f.

What will be the gravitational waveform?

History

Background & details: Shapiro & Teukolsky
Black Holes, White Dwarfs, Neutron stars

Proposed by Baade and Zwicky as formed in supernovae
(Baade and Zwicky coined super-novae in 1931!)

First neutron star models: Oppenheimer & Volkoff 1939

Expected to be small and hence undetectable via thermal radiation → no
interest for ~30 years.

This changed with the discovery of high-energy (X-ray, 1962) emission

General acceptance: discovery of pulsars in 1967

<https://www.newyorker.com/tech/elements/the-astronomer-jocelyn-bell-burnell-looks-back-on-her-cosmic-legacy>

Chandrasekhar limit by Landau 1932 --- 1.5 Msun

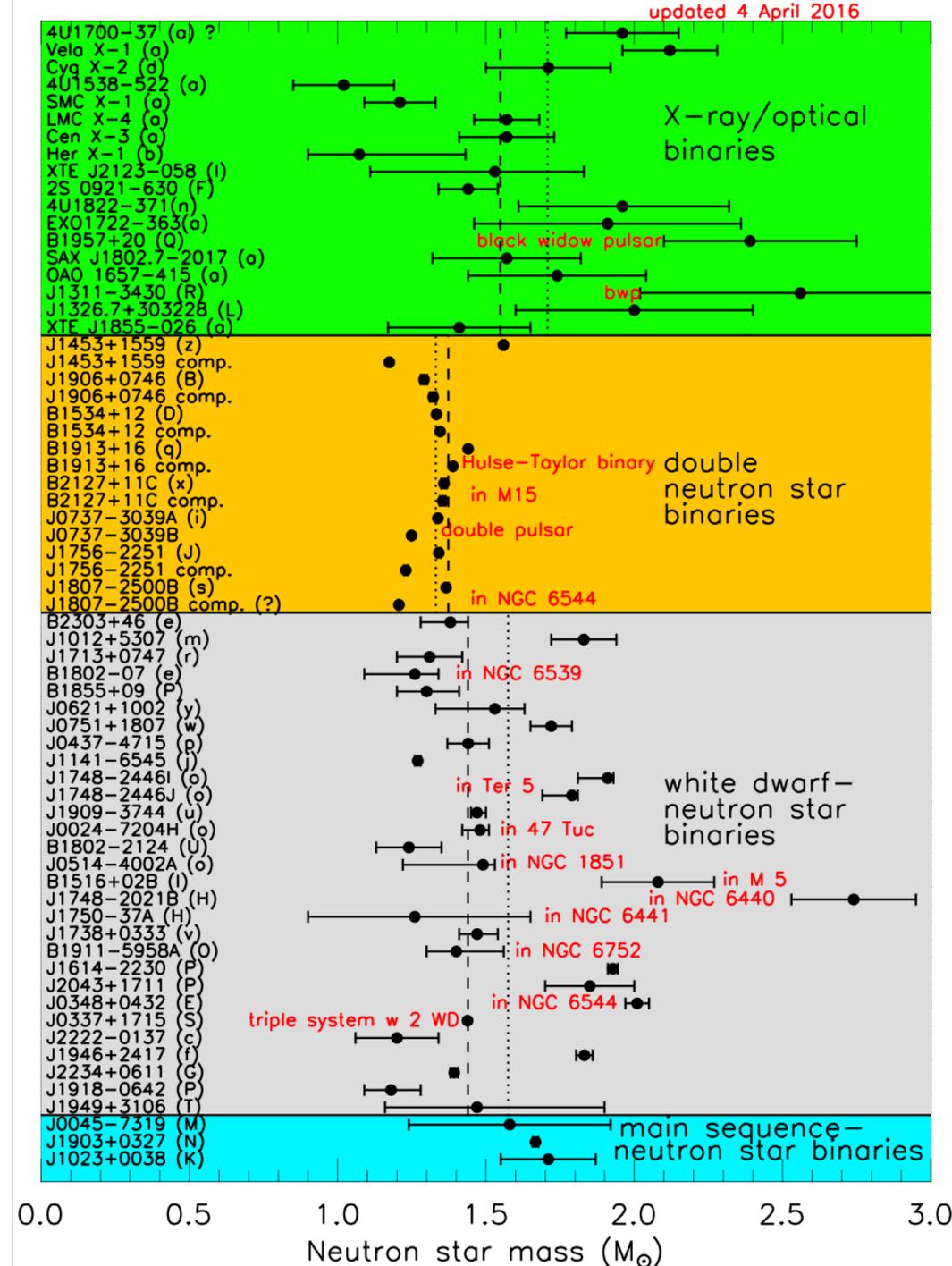
Properties - Mass

There should be a lower limit just from formation. --- 1.1 Msun

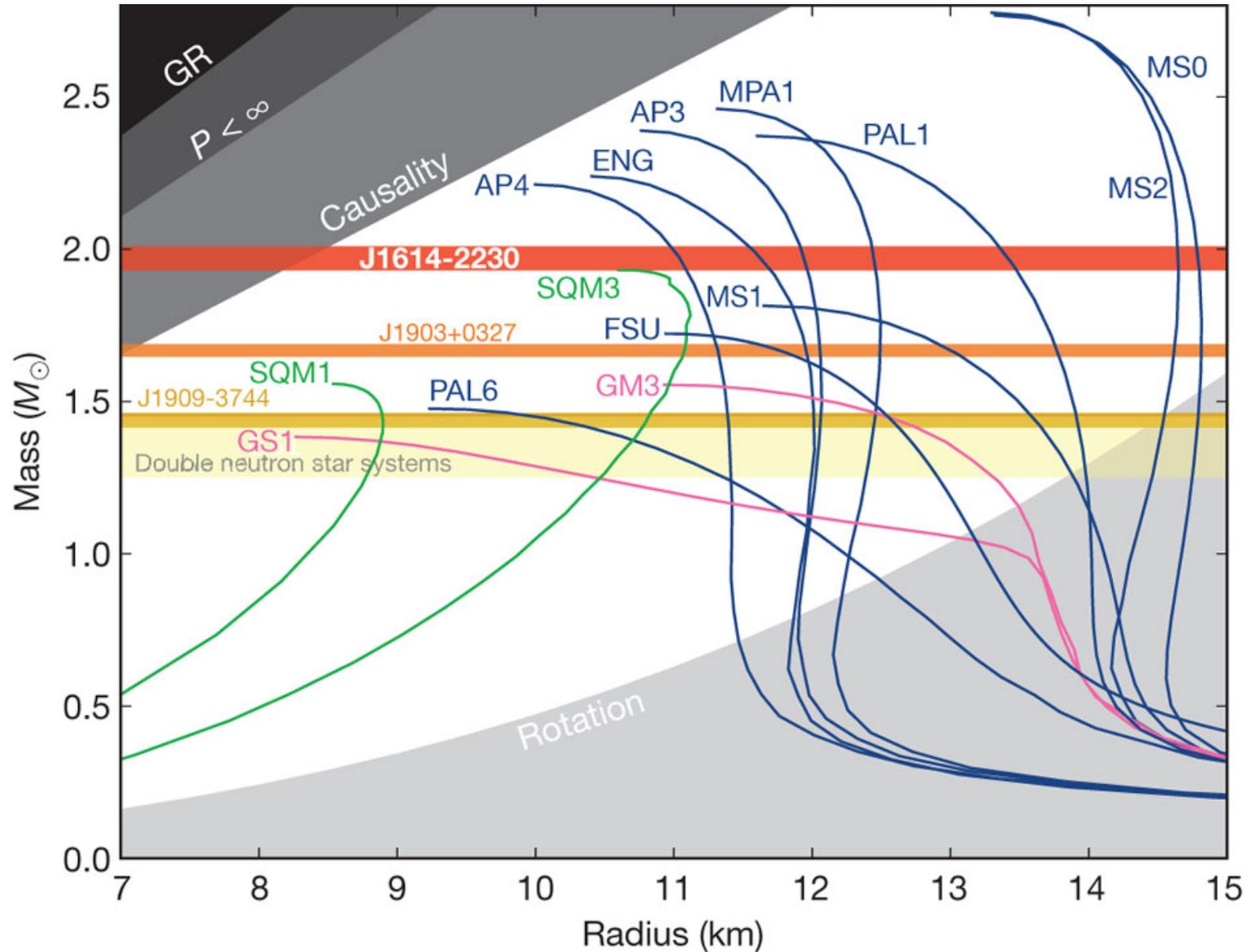
Maximum observed mass --- ~2 Msun

Maximum mass from GW170817 --- 2.17 Msun

Mass distribution depends on NS companion



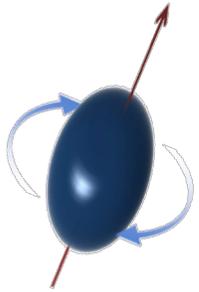
Properties – Equation of state



Magnetic field

Typically 10^4 - 10^{11} T

Newly born magnetars --- 10^{15} T

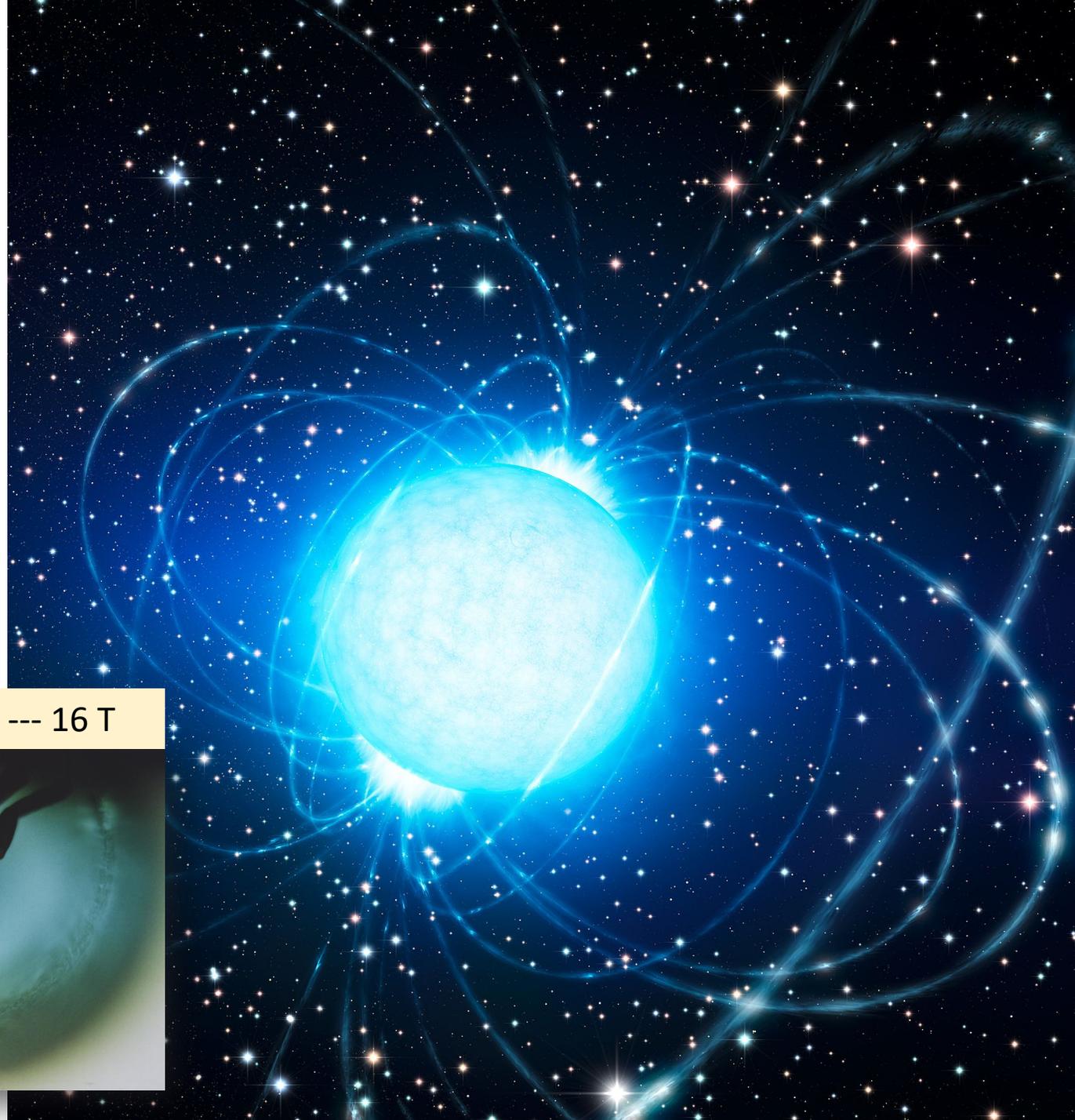


Can make NS prolate

After formation → dynamo effect
→ loss of angular momentum
↔ competing effect with GWs

NS slowly loses magnetic fields
→ weak during BNS merger

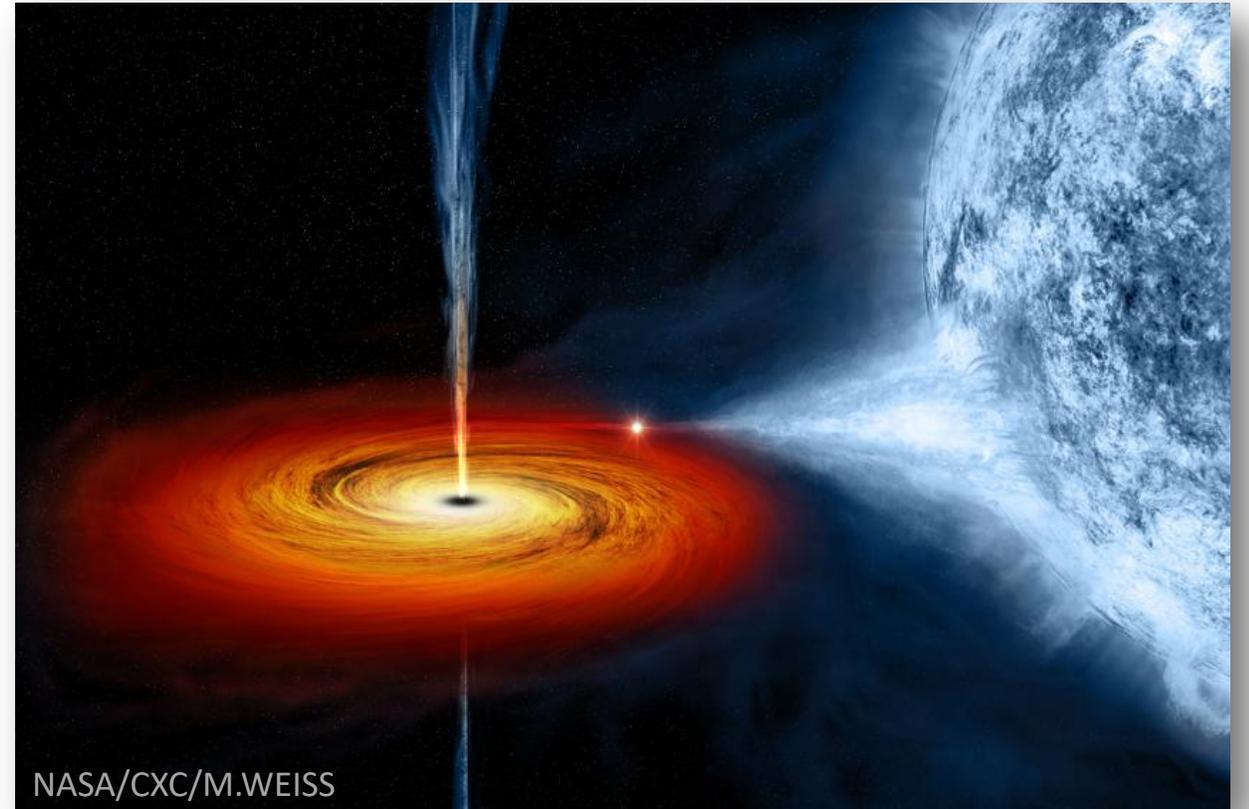
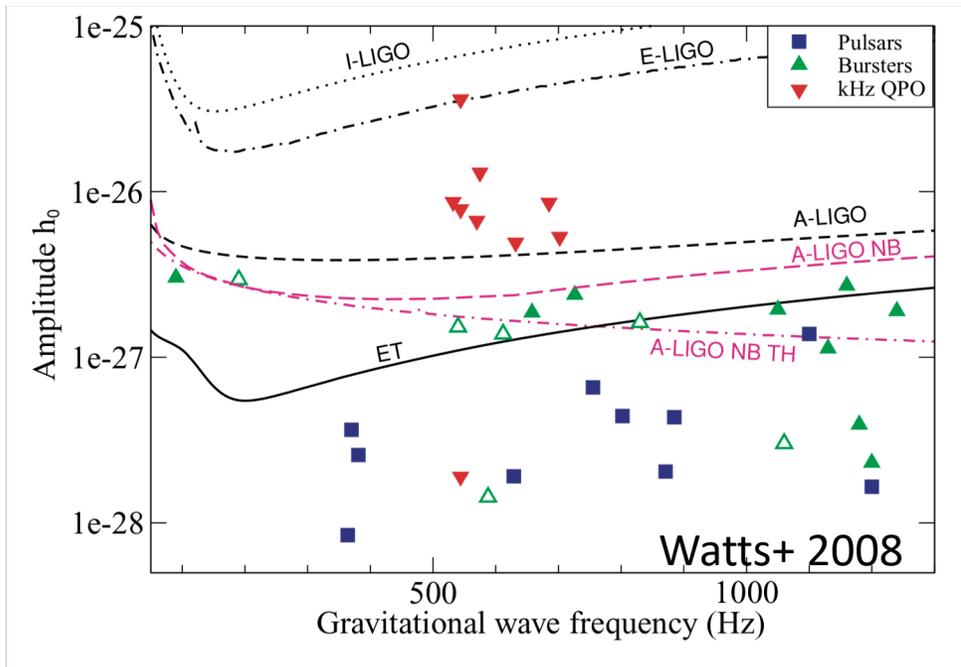
Frog levitation --- 16 T



Accretion and spindown

Many accreting NSs rotate around 300 Hz

Maybe GW emission?



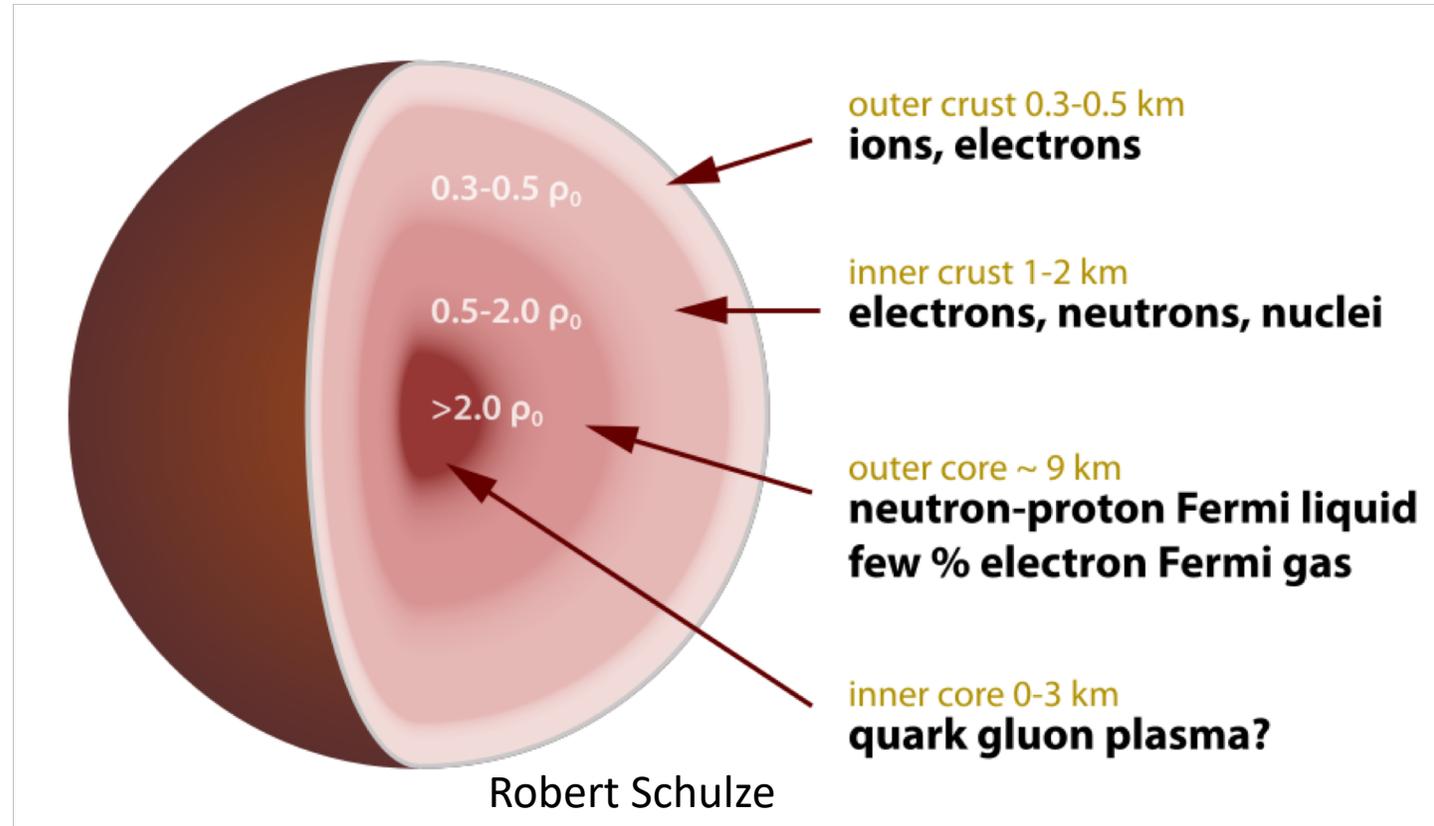
Structure

Mostly unknown

There is likely a NS “crust”

There is likely a core

Quark-gluon plasma in core?



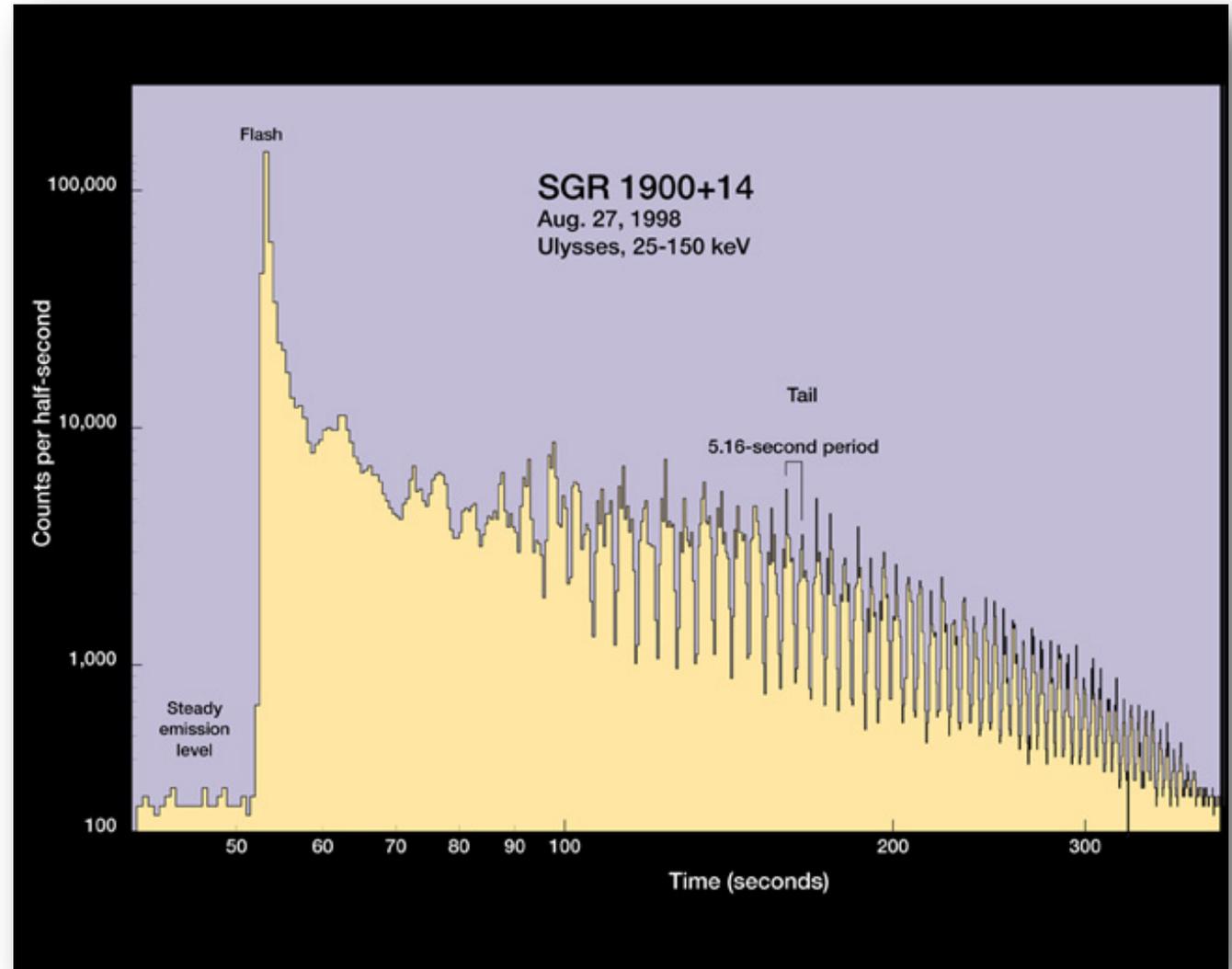
Soft gamma repeaters

Occasional outbursts of gamma rays

Quasi-periodic oscillations

Starquakes??

Magnetic field reorganization?



Glitches

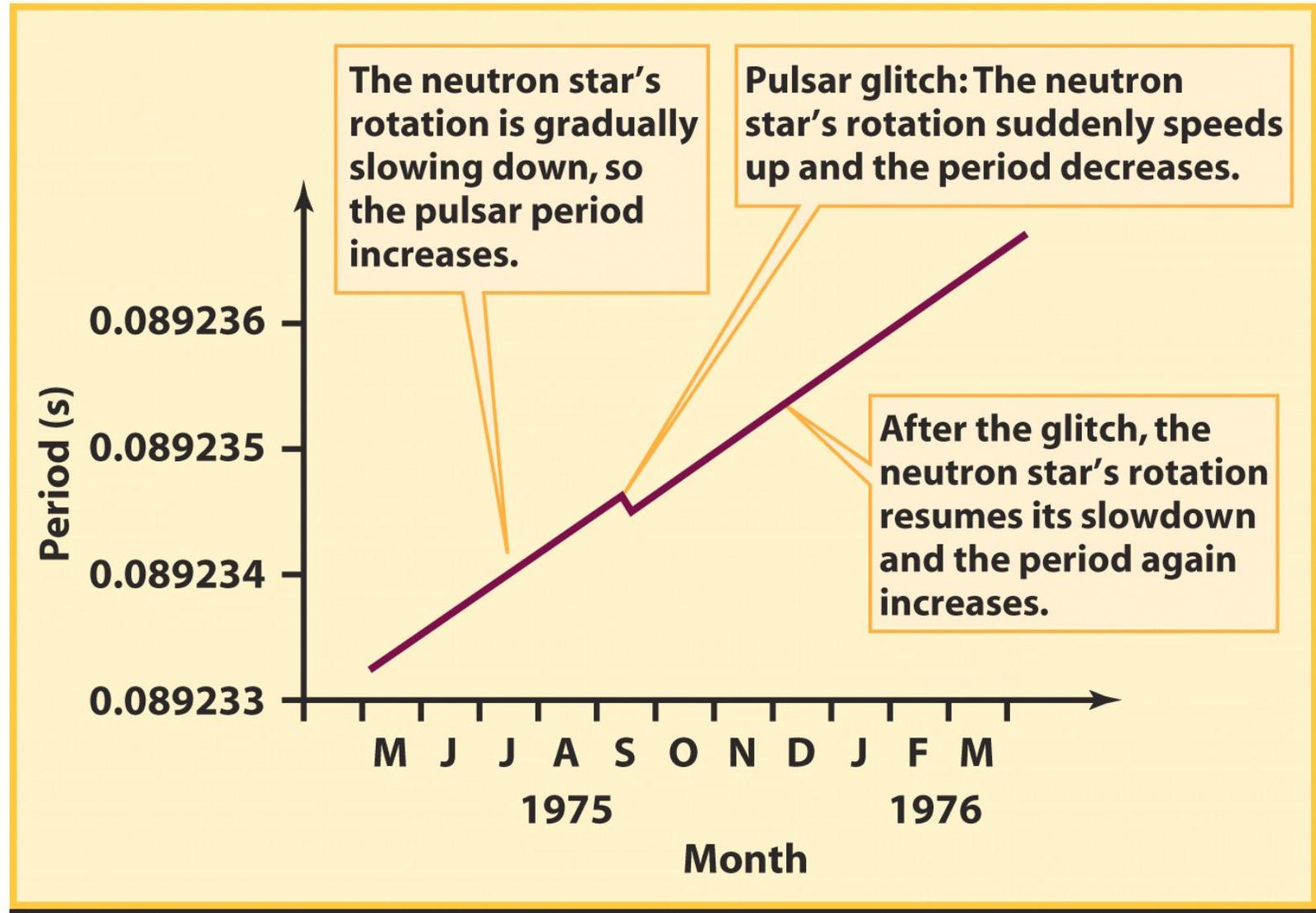
Starquakes?

NS crust ruptures
→ radius decreases
→ faster rotation

Core reorganization that
releases energy?

Anti-glitches
Unclear??

Bad for pulsar timing



Pulsars

Very regular period

Formed in a supernova

After sufficient slowdown the radio pulsar mechanism is turned off.

Energy source:

- Rotation
- Accretion
- Magnetic fields

