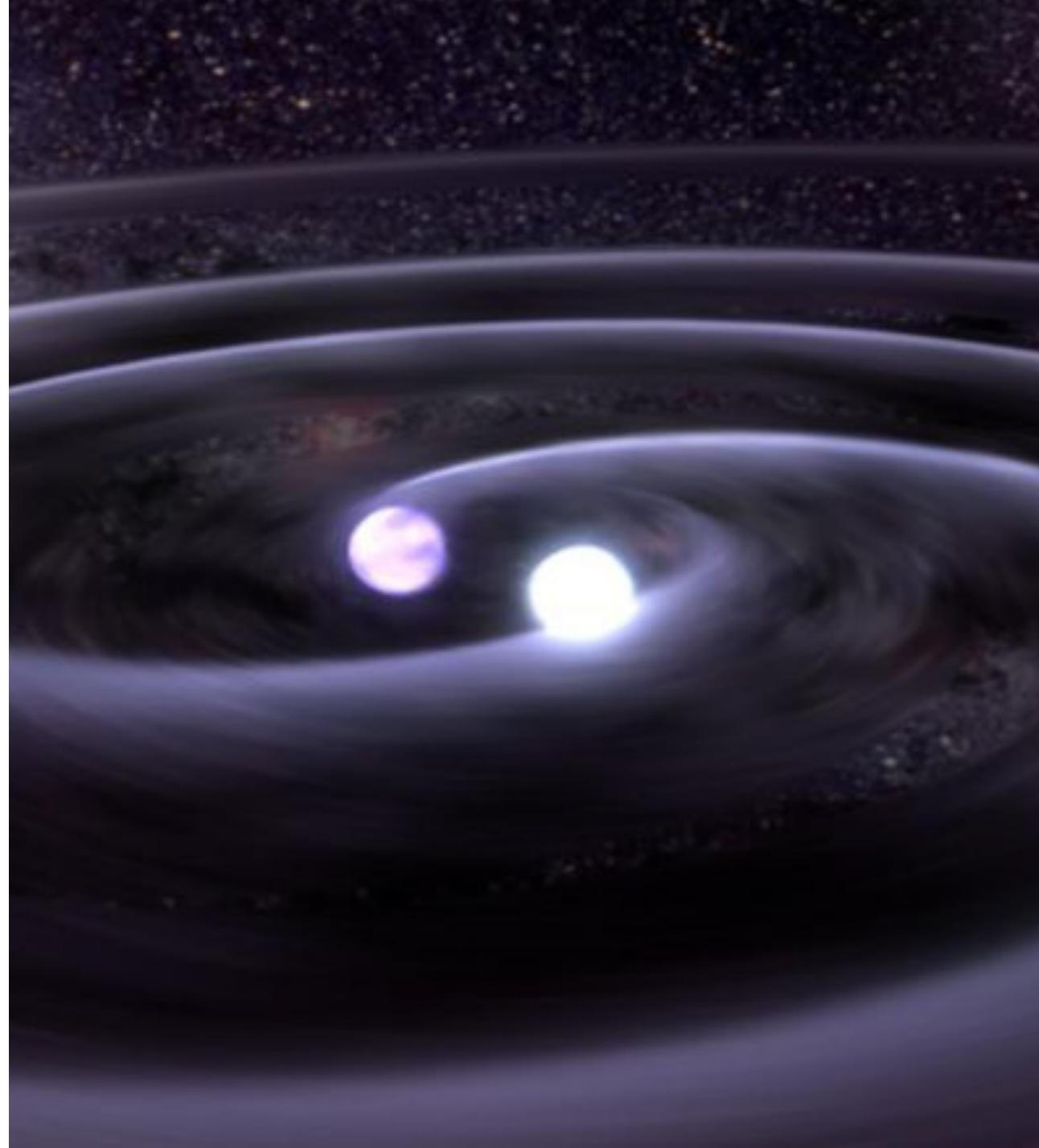


Lecture XXXV.

Gravitational Waves



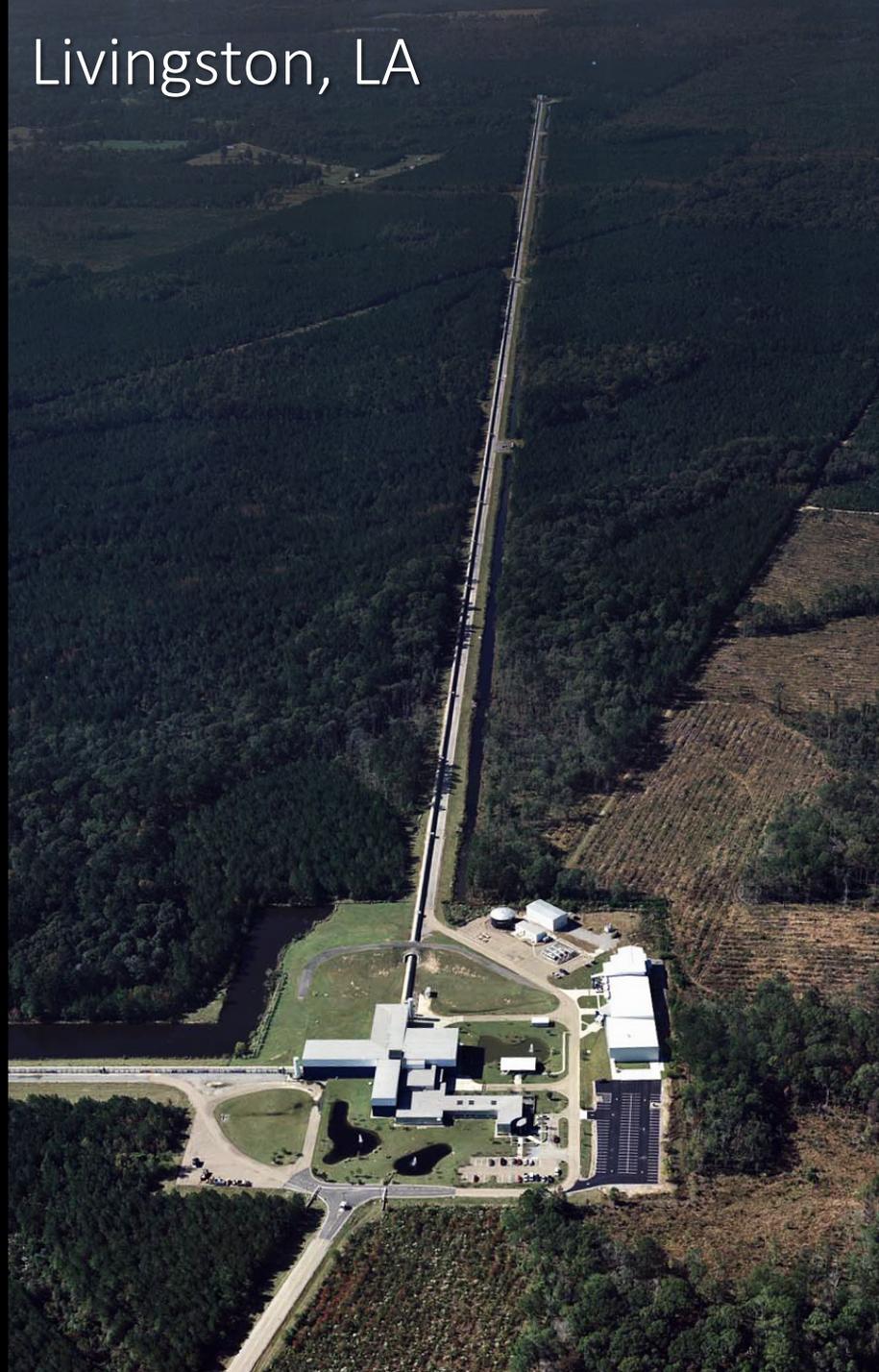
Imre Bartos | Fall 2018



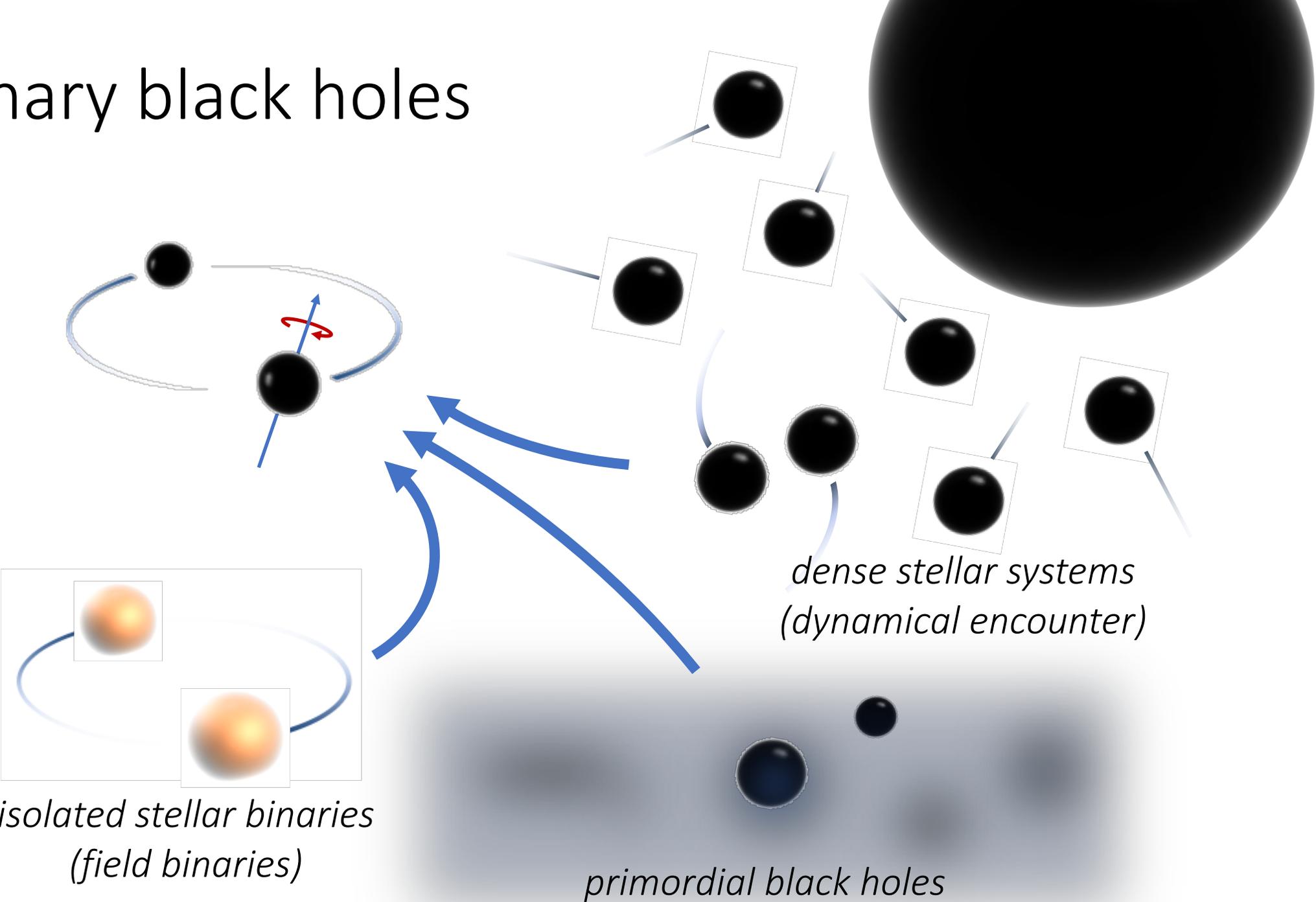
Hanford, WA



Livingston, LA



binary black holes

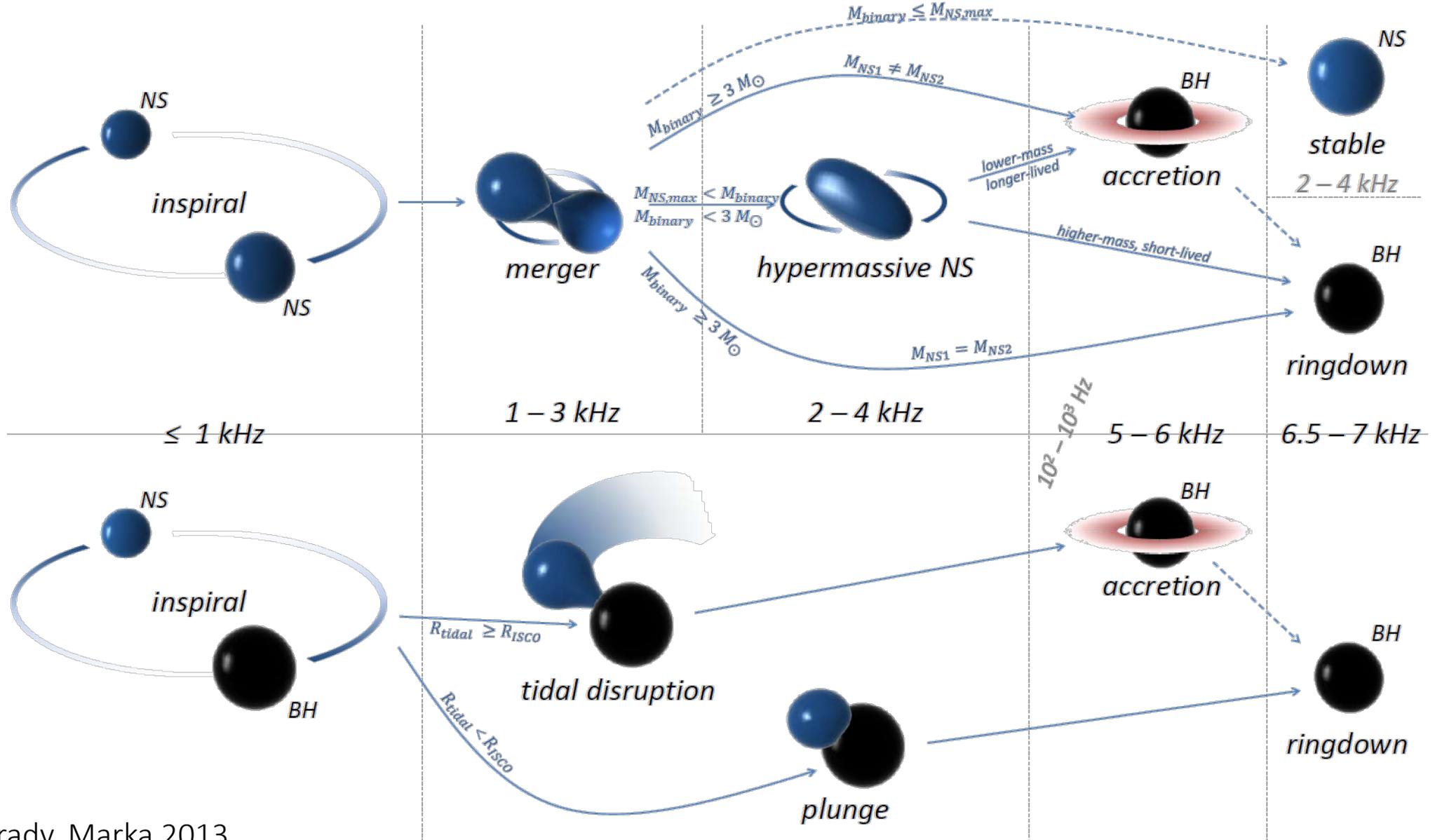


*isolated stellar binaries
(field binaries)*

*dense stellar systems
(dynamical encounter)*

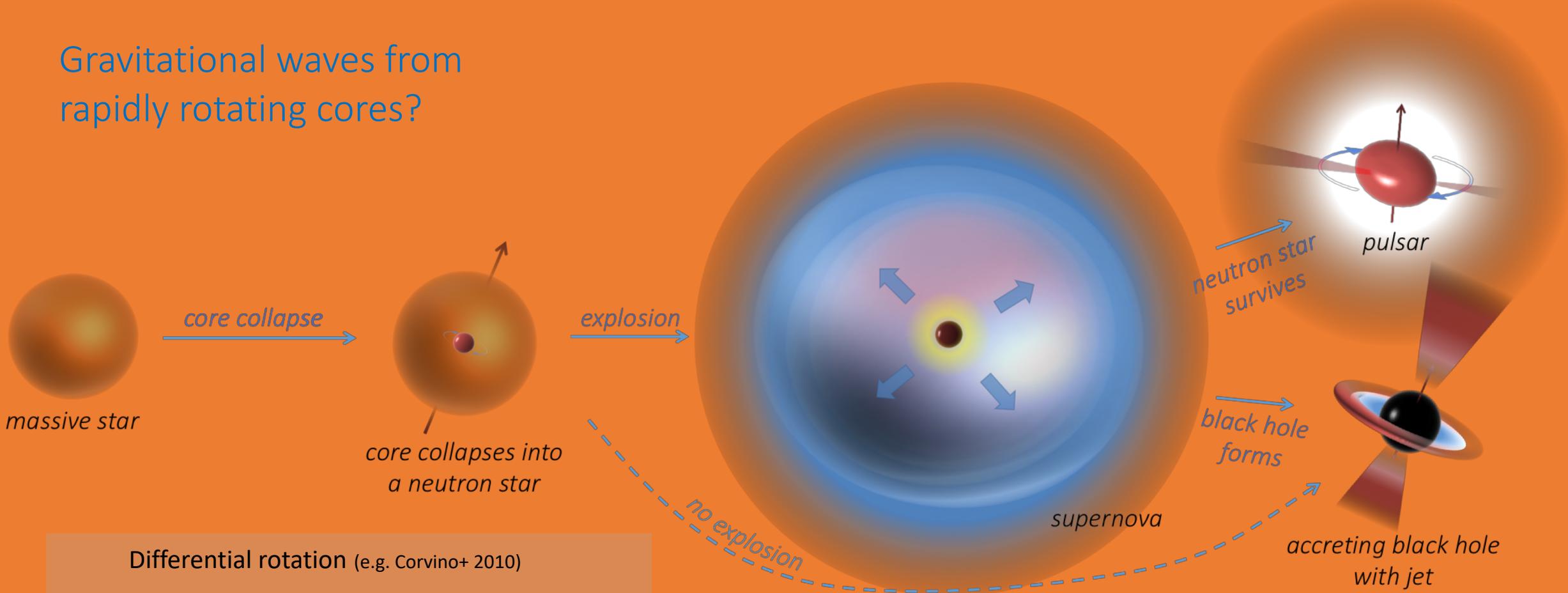
primordial black holes

progenitor: neutron star mergers



Stellar core collapse

Gravitational waves from rapidly rotating cores?

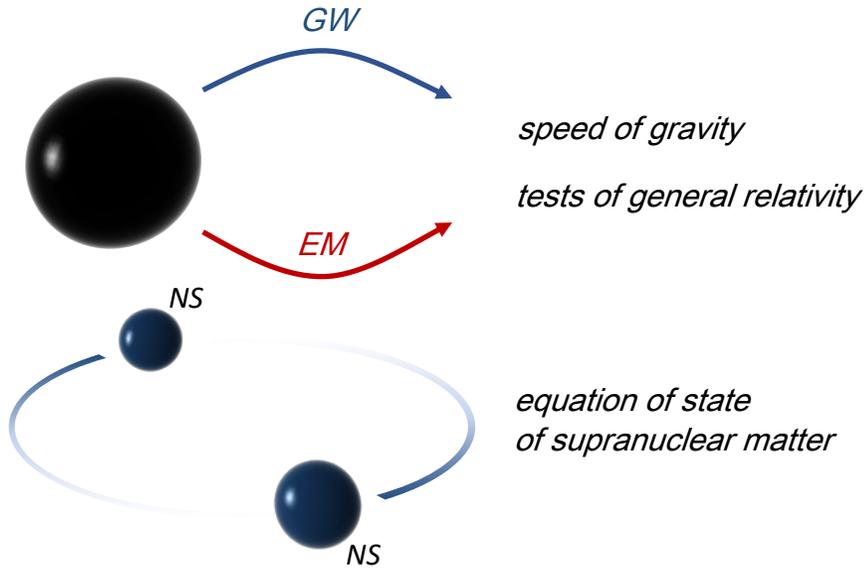


Differential rotation (e.g. Corvino+ 2010)

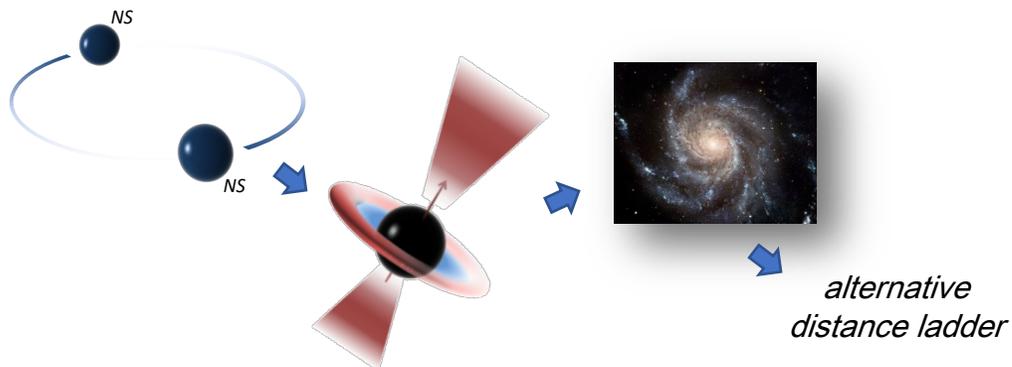
- **Dynamical instabilities** (shorter time scale)
- **Secular instabilities** (longer time scale)
- **Magnetic distortion**

Fallback accretion? (Piro & Thrane, 2012)

Fundamental physics

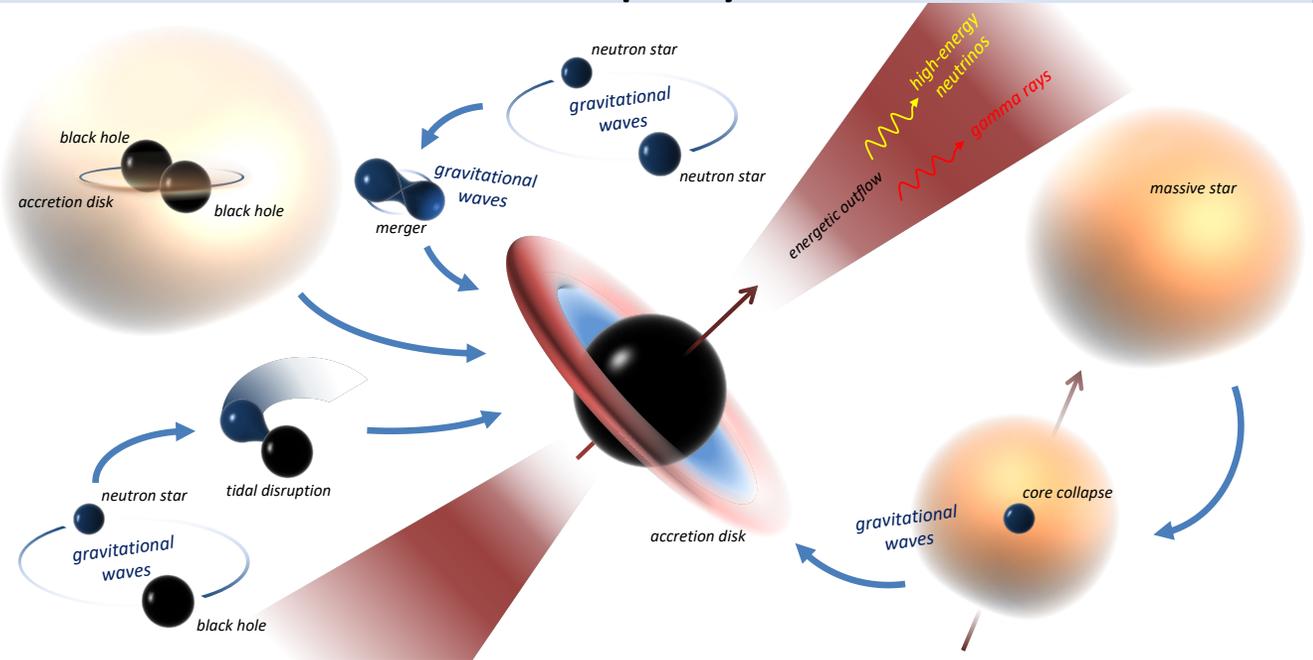


Cosmology



Science targets

Astrophysics



- *Black hole accretion*
- *Cosmic particle acceleration*
- *Stellar core collapse*
- *Compact binary formation channels*
- *Intermediate mass black holes*

- *Origin of heavy elements*
- *Environment in galactic nuclei*
- *Relativistic outflows*
- *...*

Search for gravitational waves

Rotating source:

$$h_+(t) = \frac{1}{2}(1 + \cos^2(\iota)) A(t) \cos \Phi(t)$$
$$h_\times(t) = \cos(\iota) A(t) \sin \Phi(t),$$

Root-sum-square amplitude:

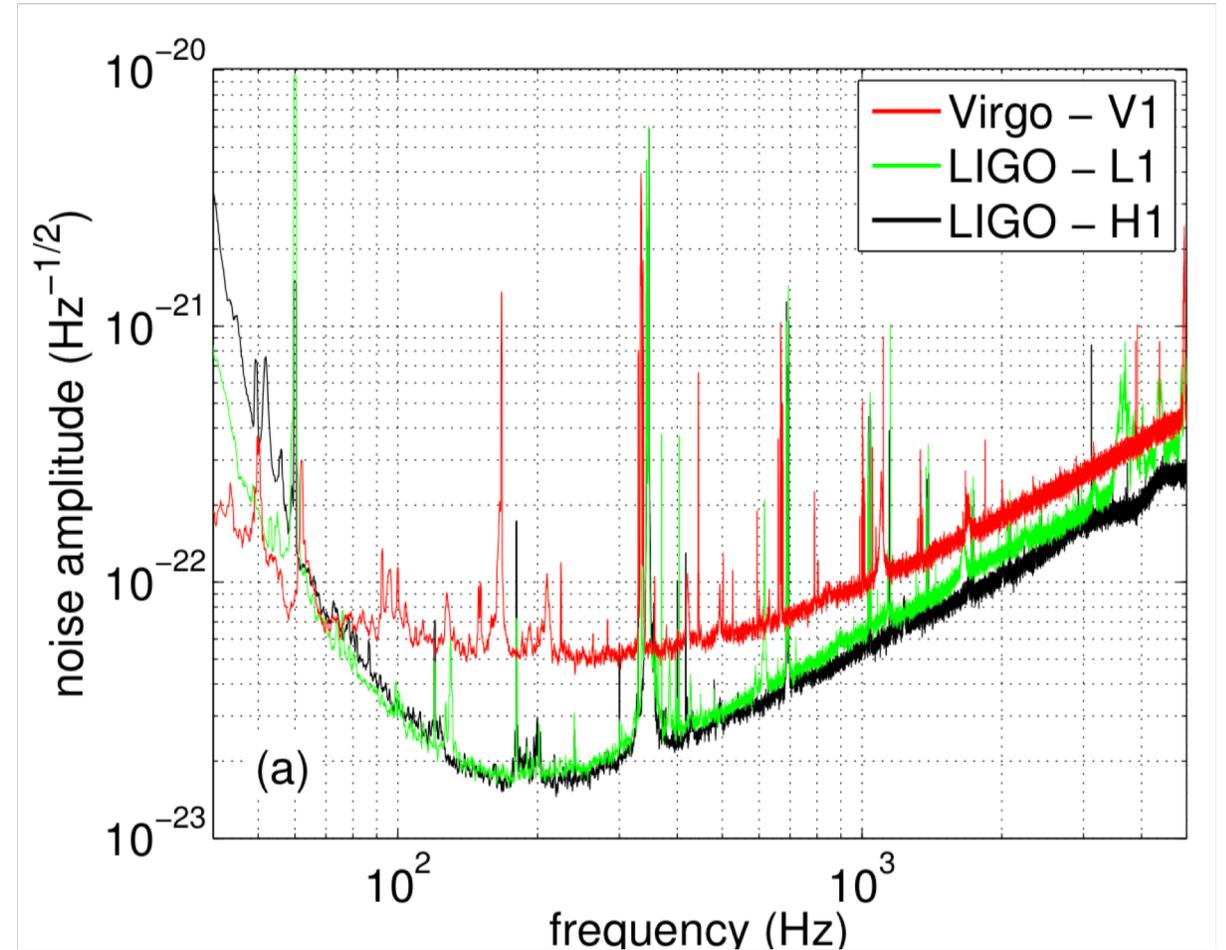
$$h_{\text{rss}} = \int_{-\infty}^{\infty} dt [h_+^2(t) + h_\times^2(t)]$$
$$= 2 \int_0^{\infty} df [|\tilde{h}_+(f)|^2 + |\tilde{h}_\times(f)|^2]$$

Radiated GW energy:

$$E_{\text{GW}} = \frac{2}{5} \frac{\pi^2 c^3}{G} r^2 f_0^2 h_{\text{rss}}^2$$

Signal to noise ratio:

$$\rho^2 = 2 \int_{-\infty}^{\infty} df \frac{|F_+ \tilde{h}_+(f) + F_\times \tilde{h}_\times(f)|^2}{S(f)}$$



Gravitational wave sources and searches

1. Transient, unmodeled (e.g. supernova)

Prof. Klimenko

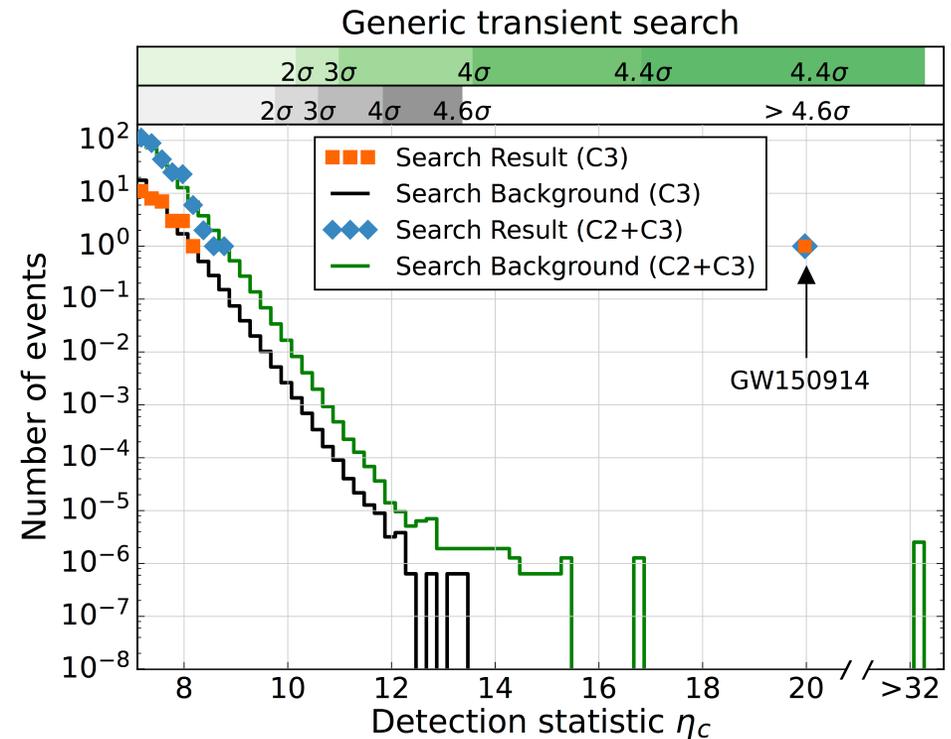
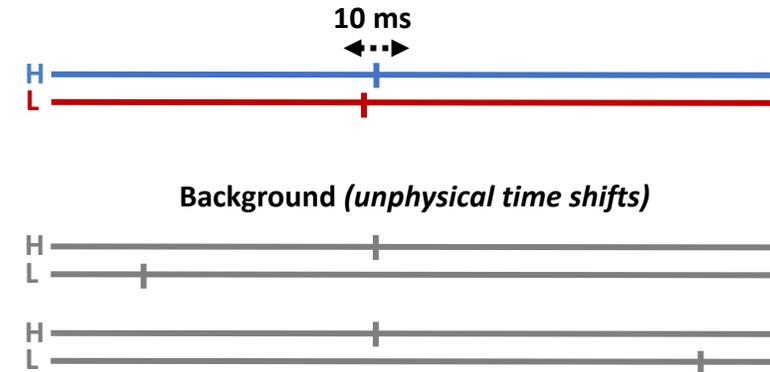
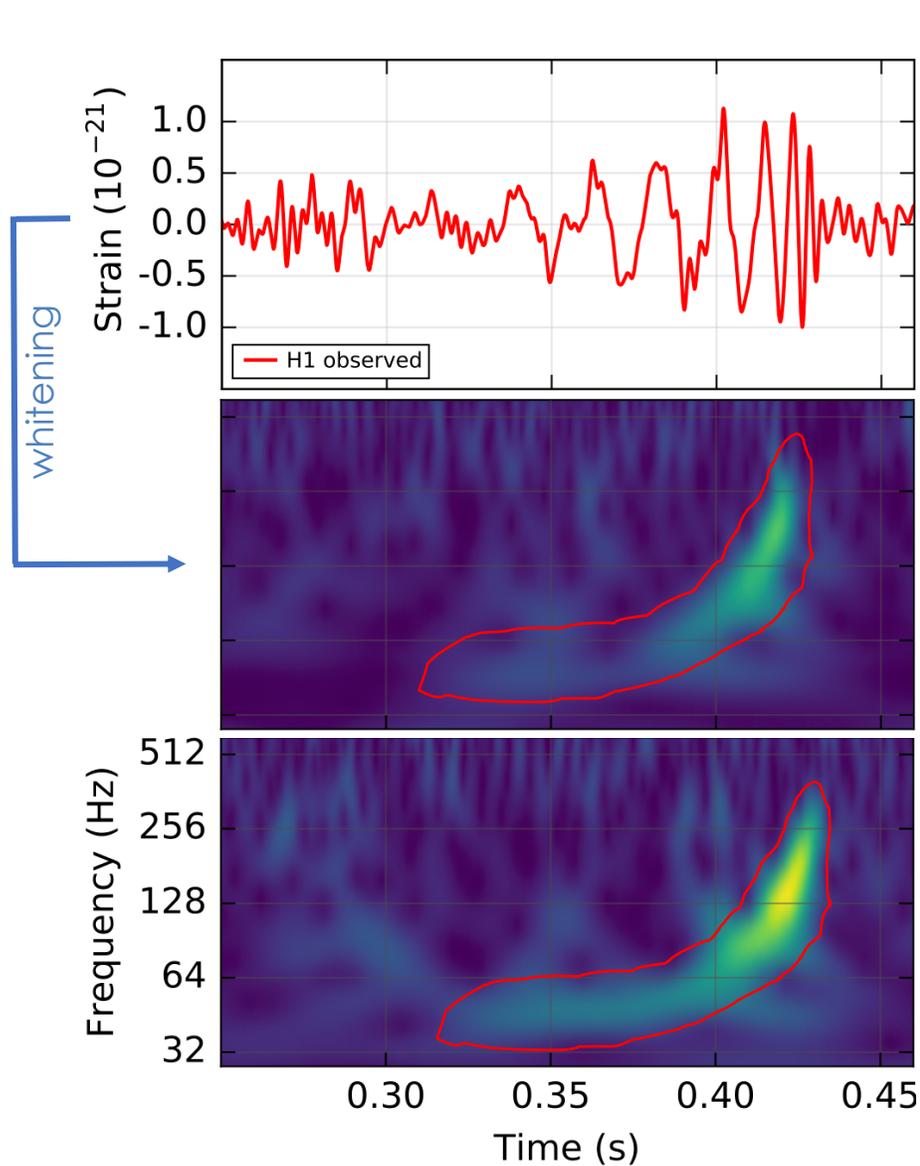
2. Transient, modeled (e.g. binary black hole merger)

(Prof. Klimenko)

3. Continuous (e.g. deformed rotating neutron star)

4. Stochastic (e.g. many distant events that are individually unresolvable)

Generic transient search



Binary coalescence search

15 (+2) parameters

masses (2)

distance (1)

direction (2)

orientation (2)

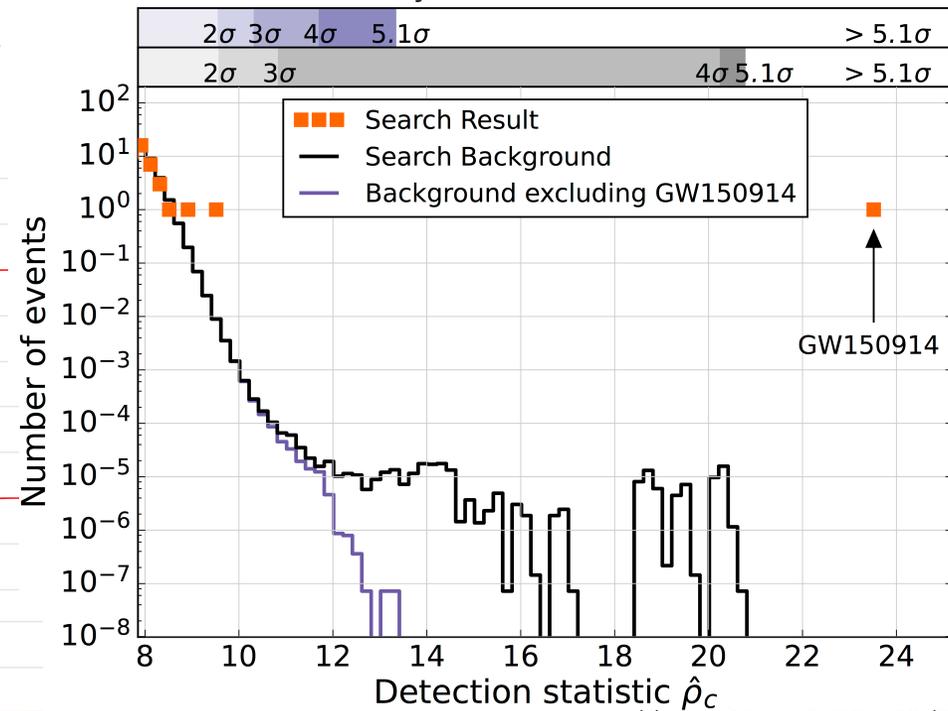
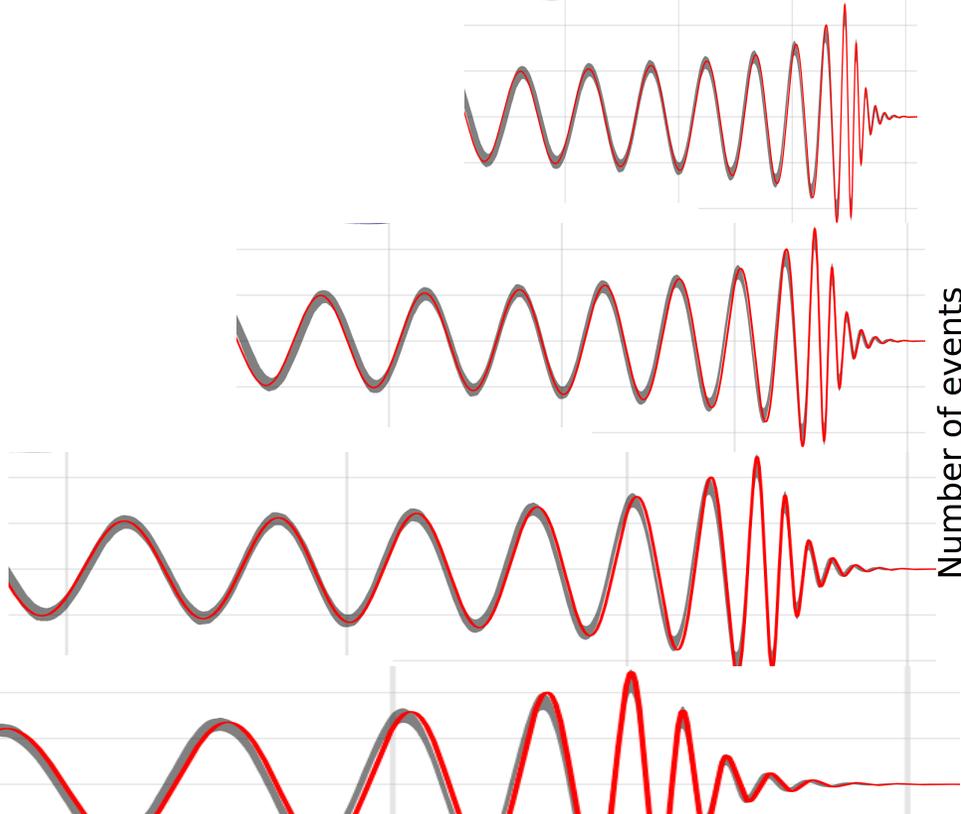
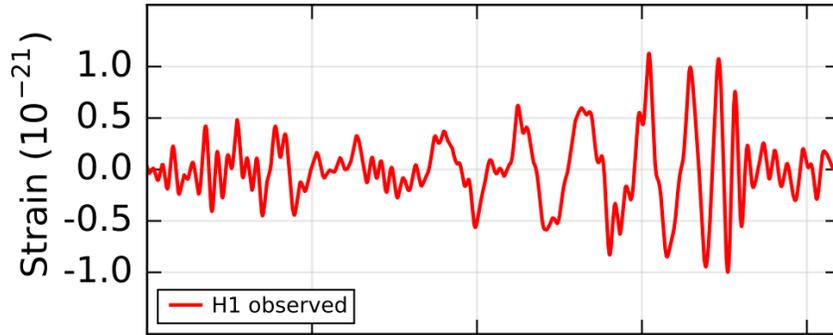
spin (6)

time (1)

phase (1)

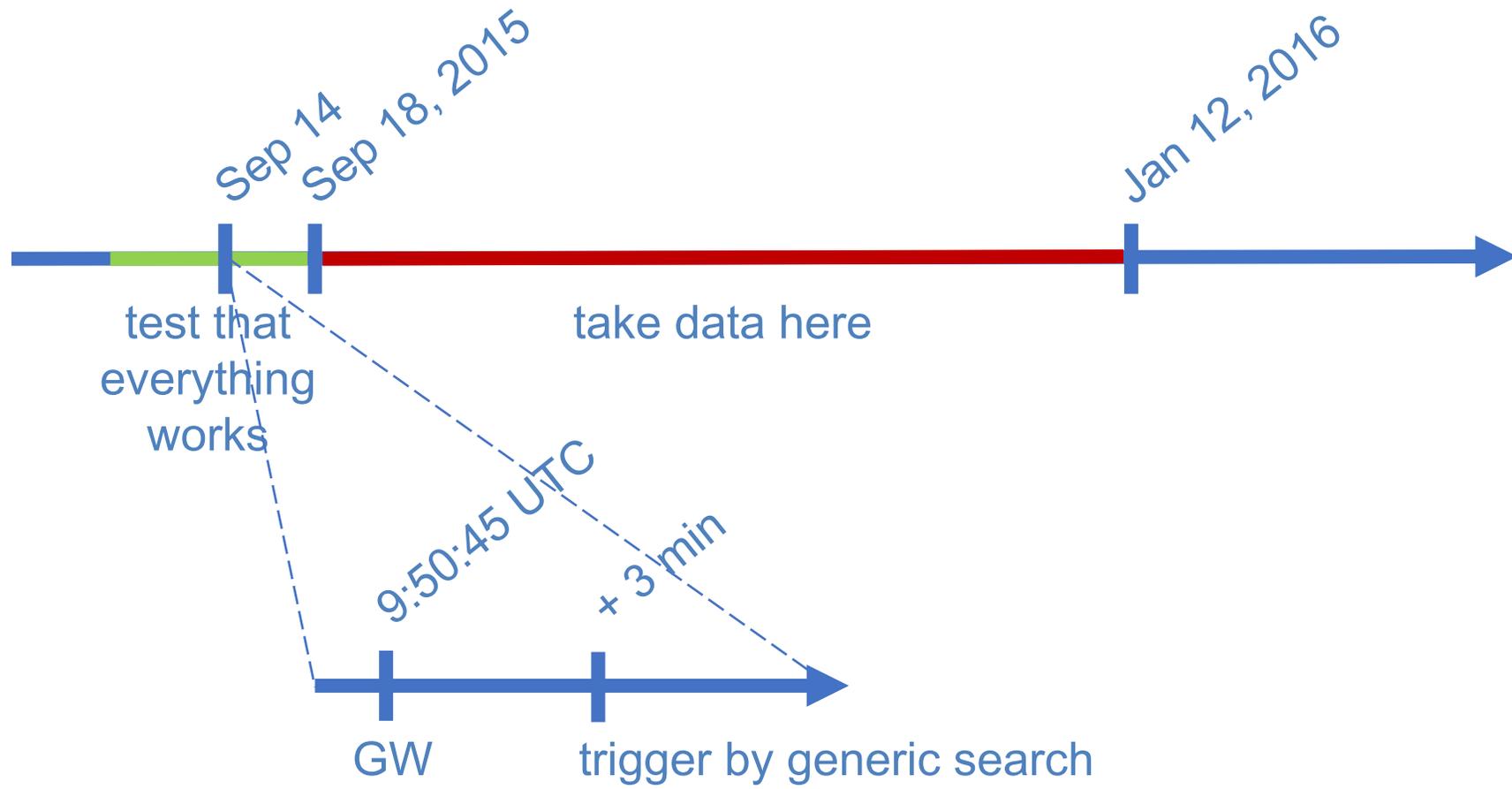
+ *eccentricity (2)*

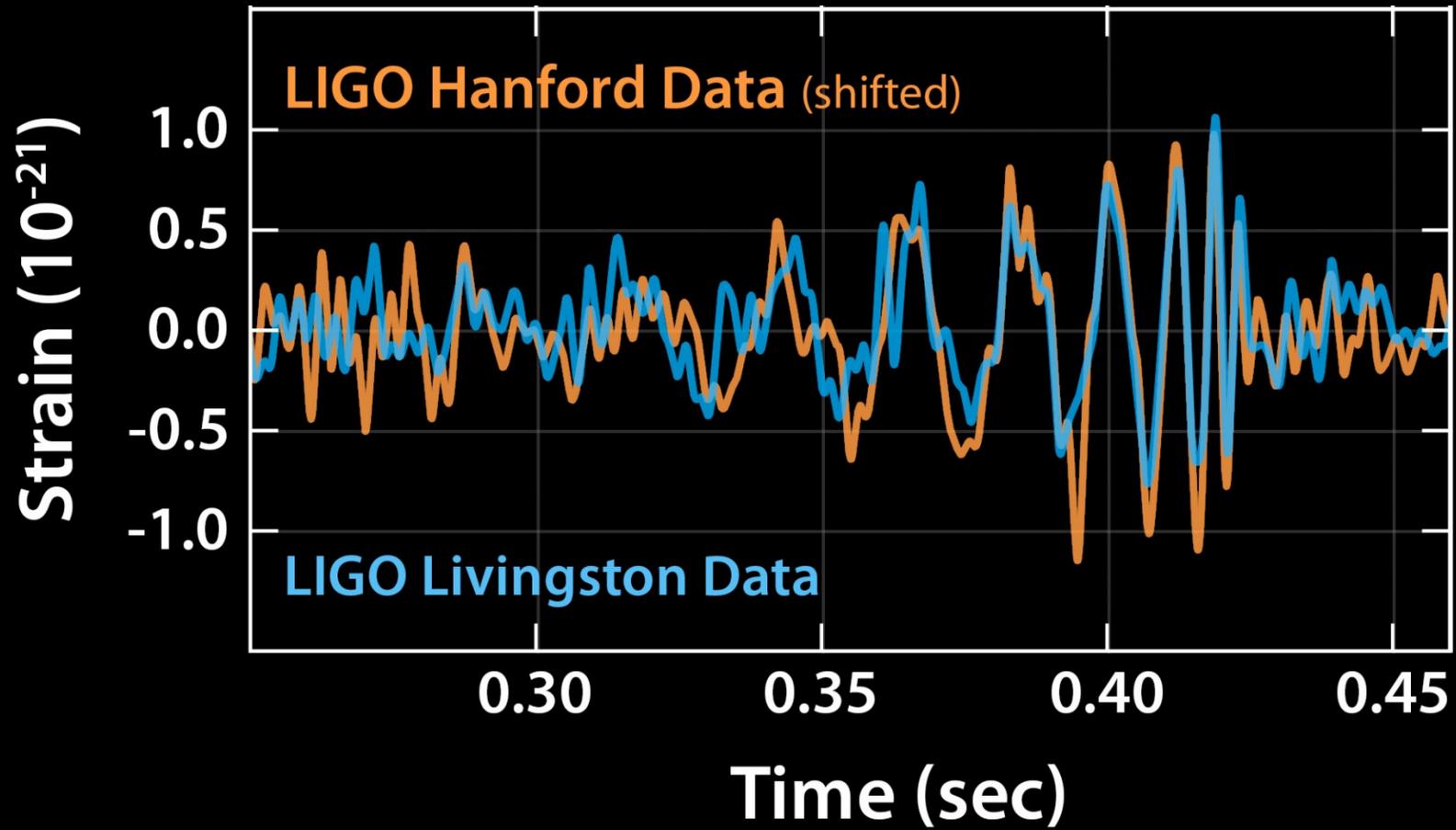
+ *calibration uncertainty (~10%)*



September 14th, 2015

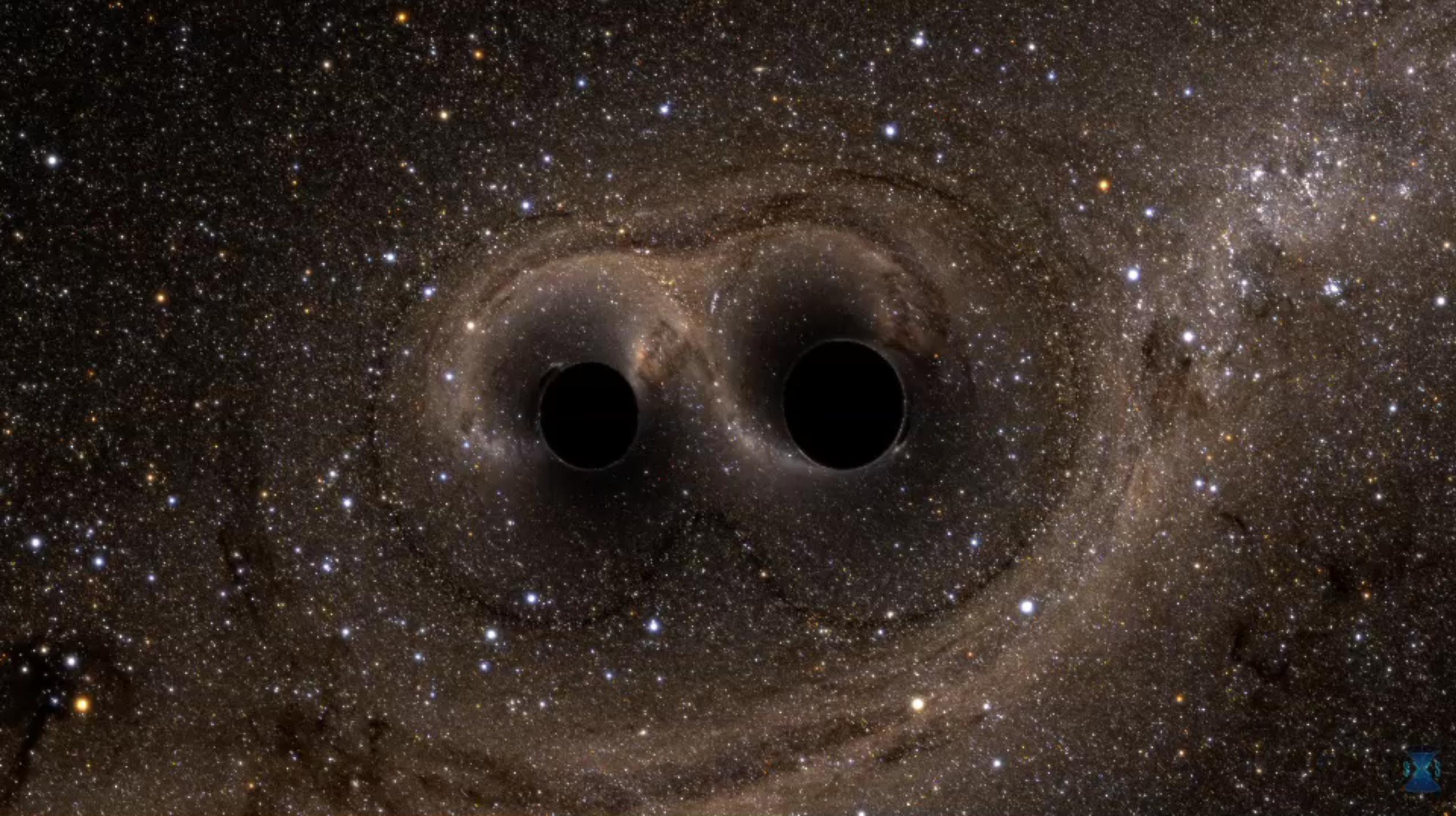
timeline

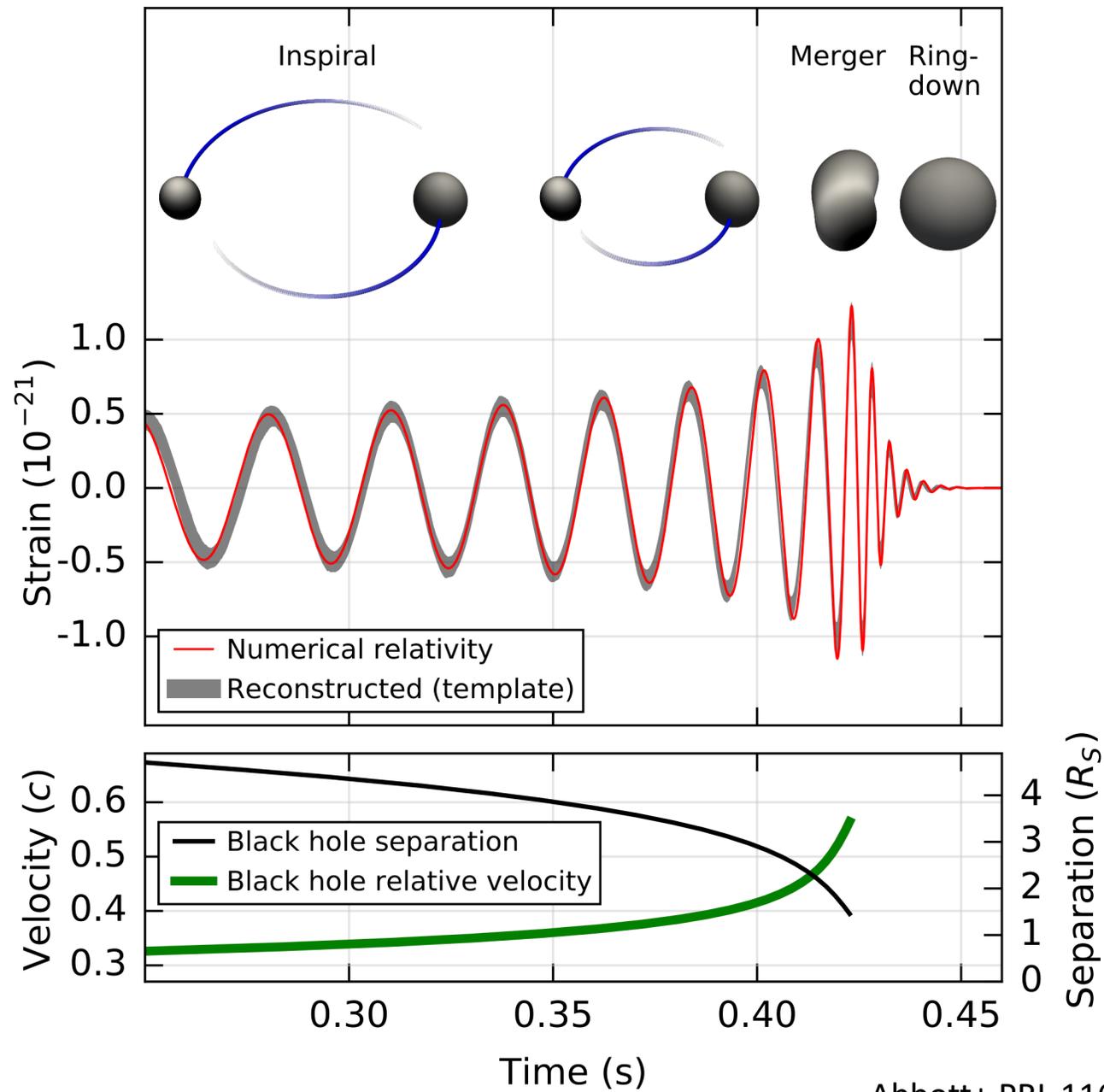






Courtesy of Corey Gray





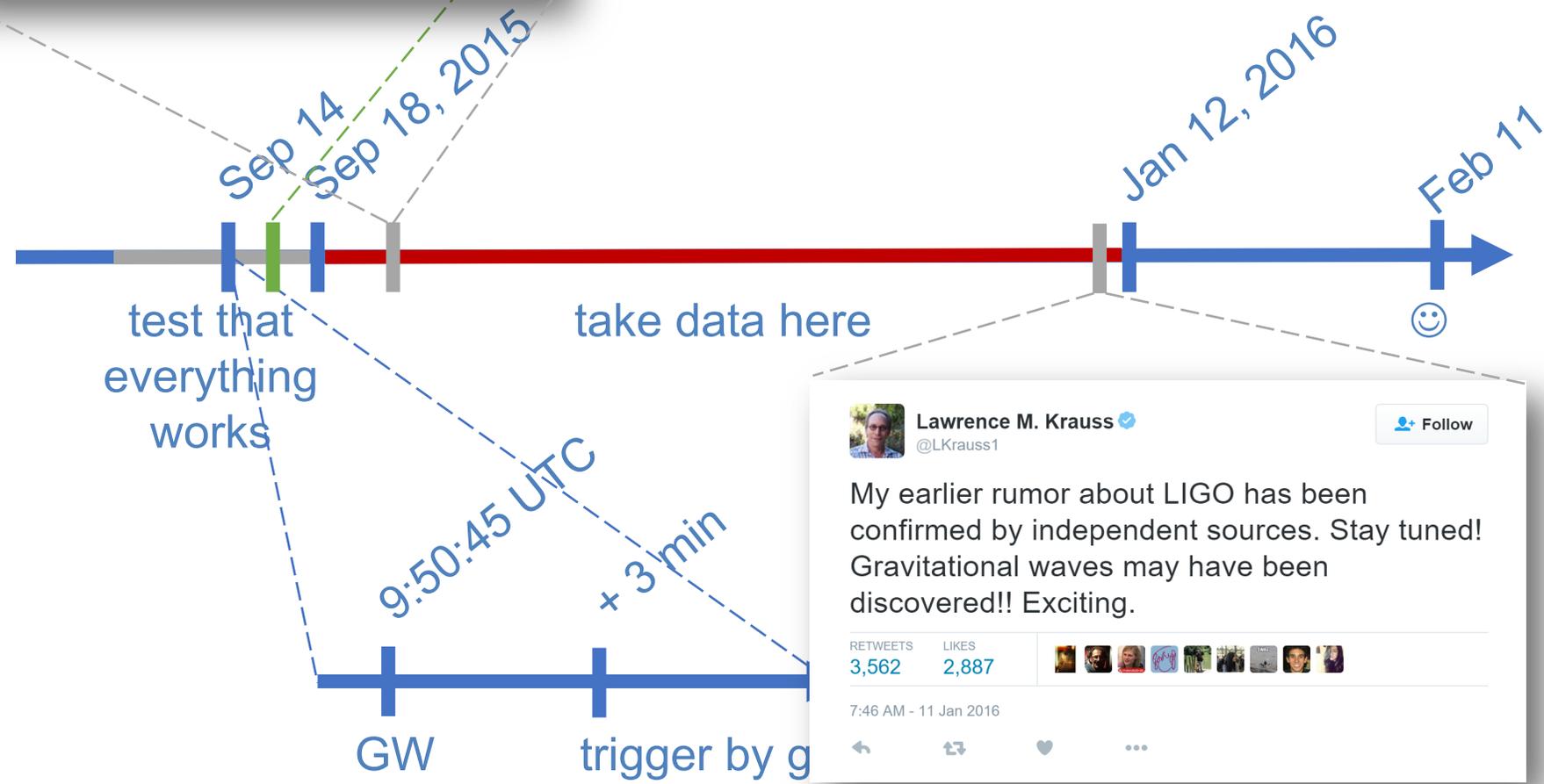
Lawrence M. Krauss  [@LKrauss1](#) 

Rumor of a gravitational wave detection at LIGO detector. Amazing if true. Will post details if it survives.

RETWEETS 636 LIKES 666 

1:39 PM - 25 Sep 2015

and initial results sent to astronomers



Lawrence M. Krauss  [@LKrauss1](#) 

My earlier rumor about LIGO has been confirmed by independent sources. Stay tuned! Gravitational waves may have been discovered!! Exciting.

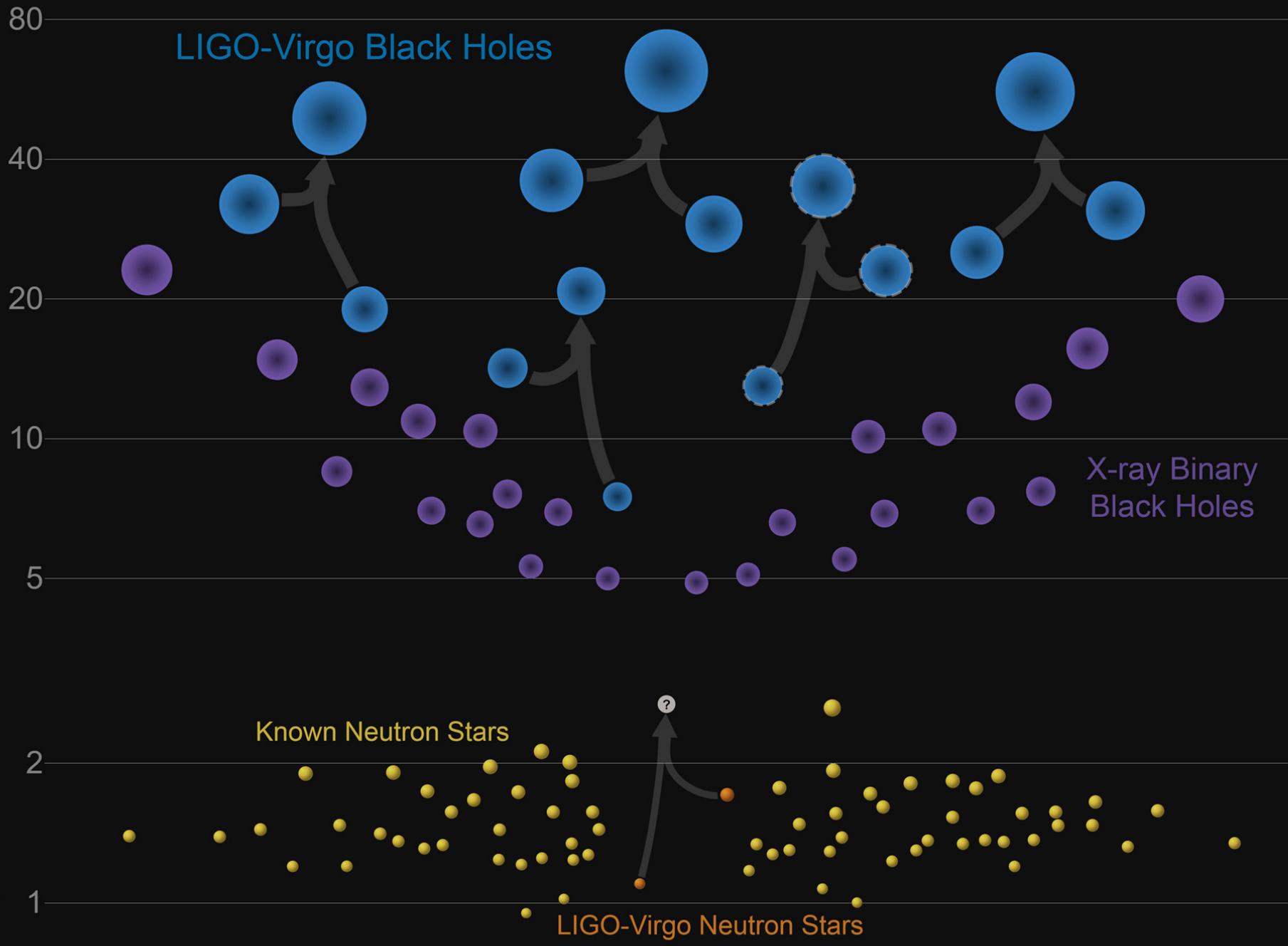
RETWEETS 3,562 LIKES 2,887 

7:46 AM - 11 Jan 2016

What have we discovered?

- Einstein was right
- First signal: “I come from a black hole”





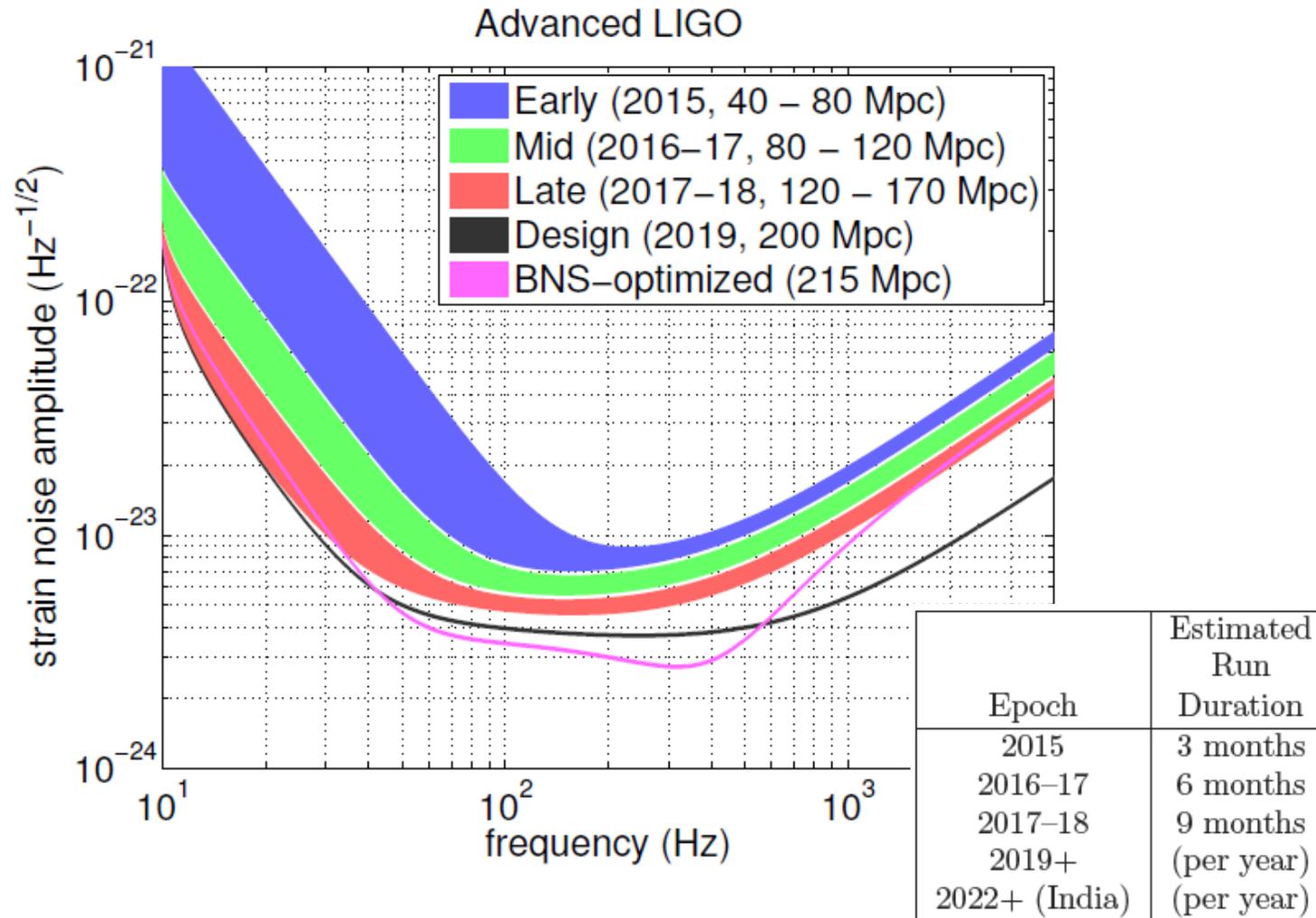
LIGO-Virgo Black Holes

X-ray Binary
Black Holes

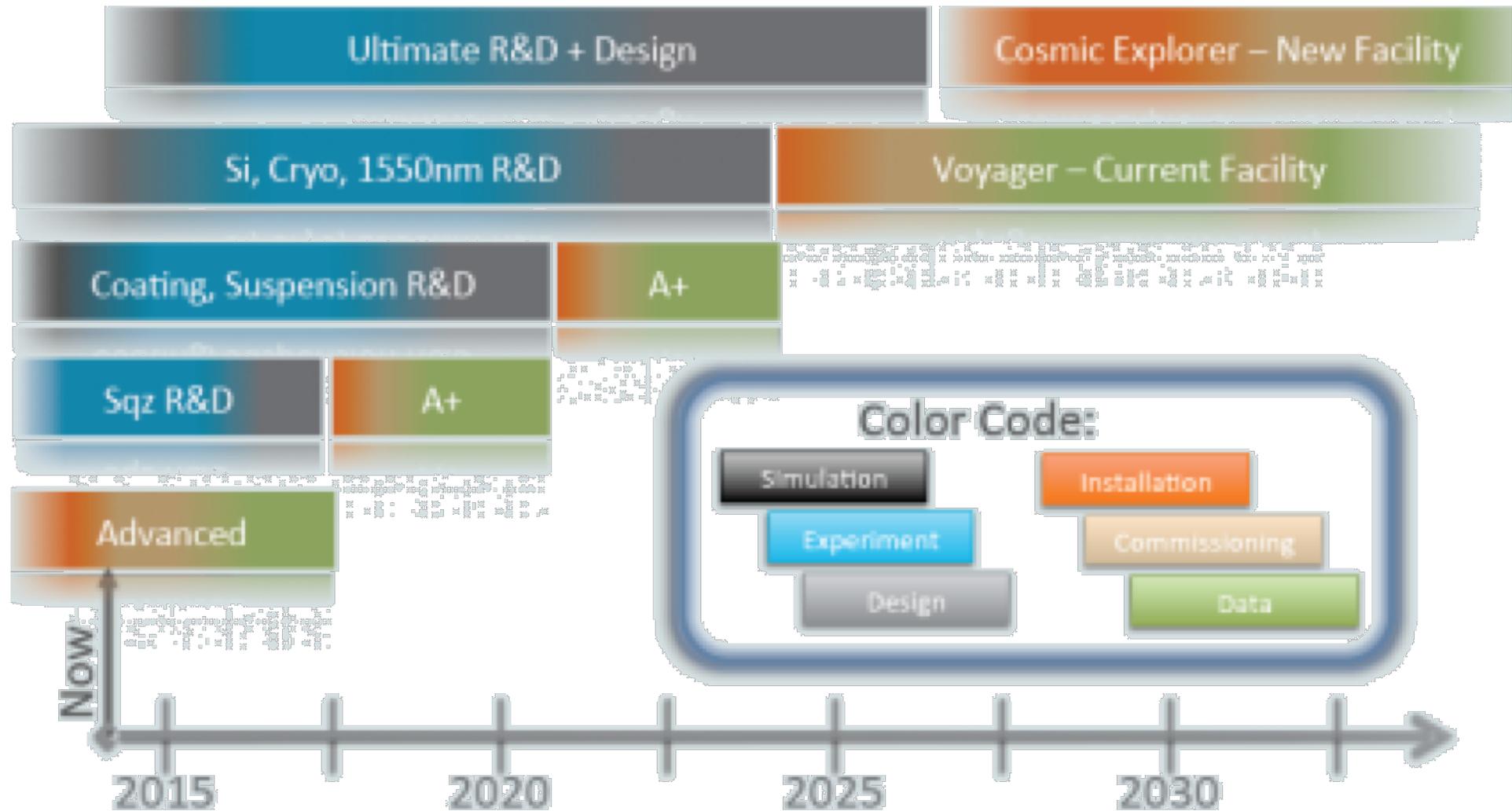
Known Neutron Stars

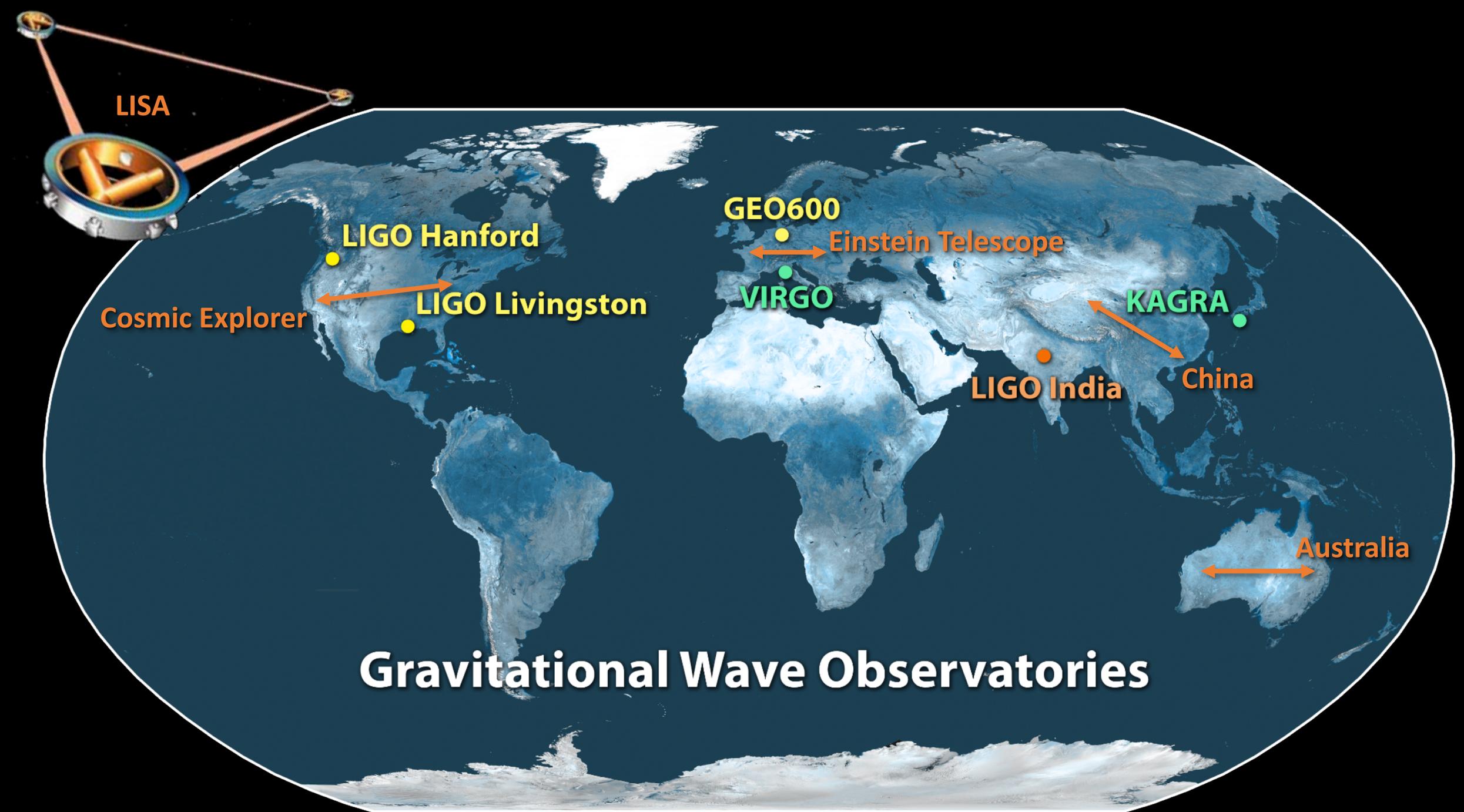
LIGO-Virgo Neutron Stars

SENSITIVITY TIMELINE

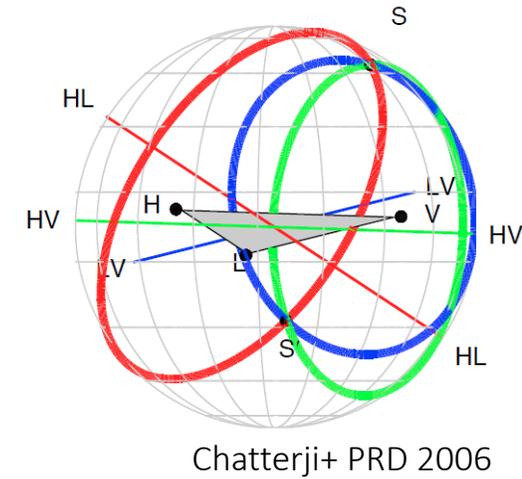
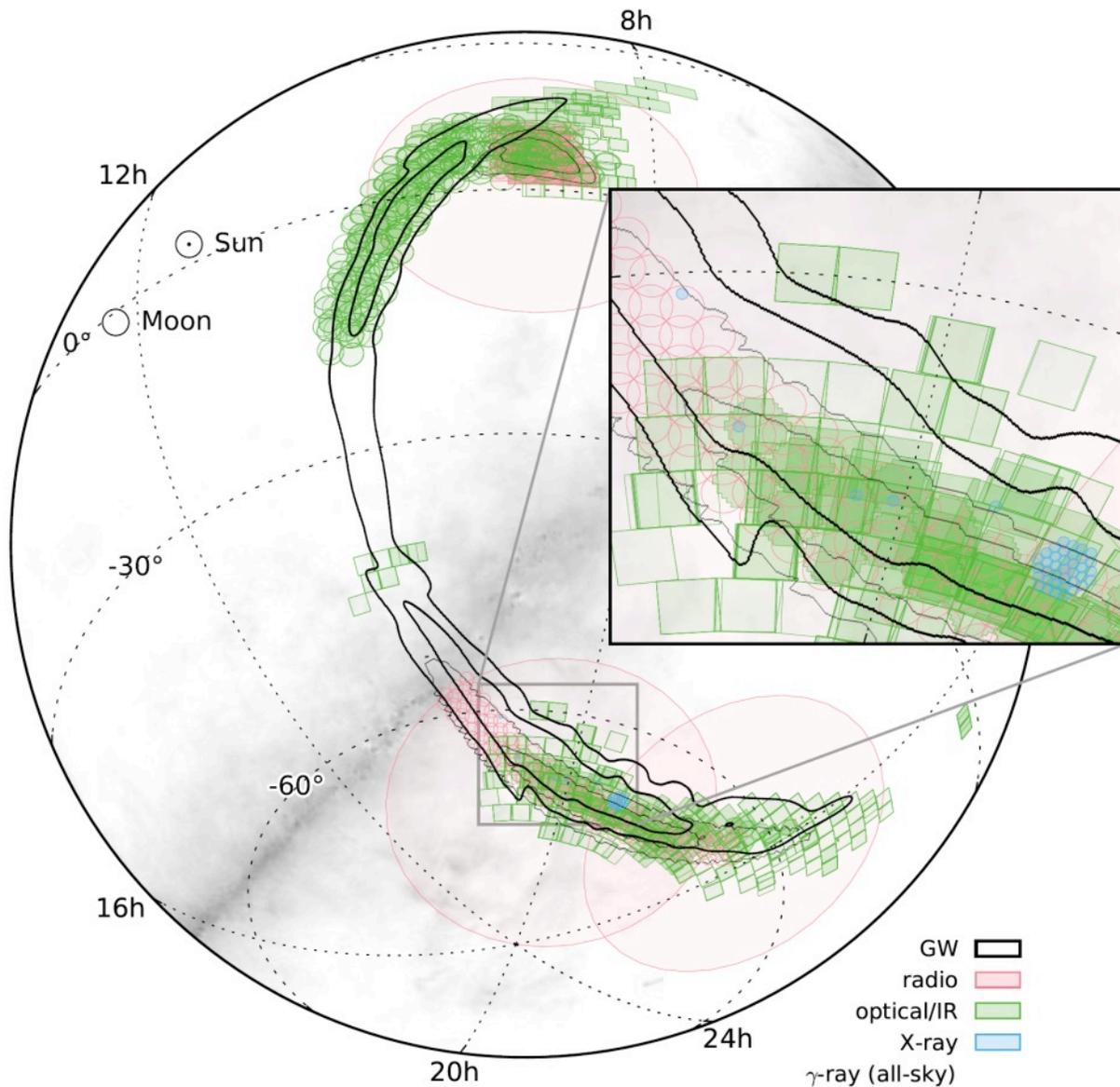


LIGO upgrade timeline



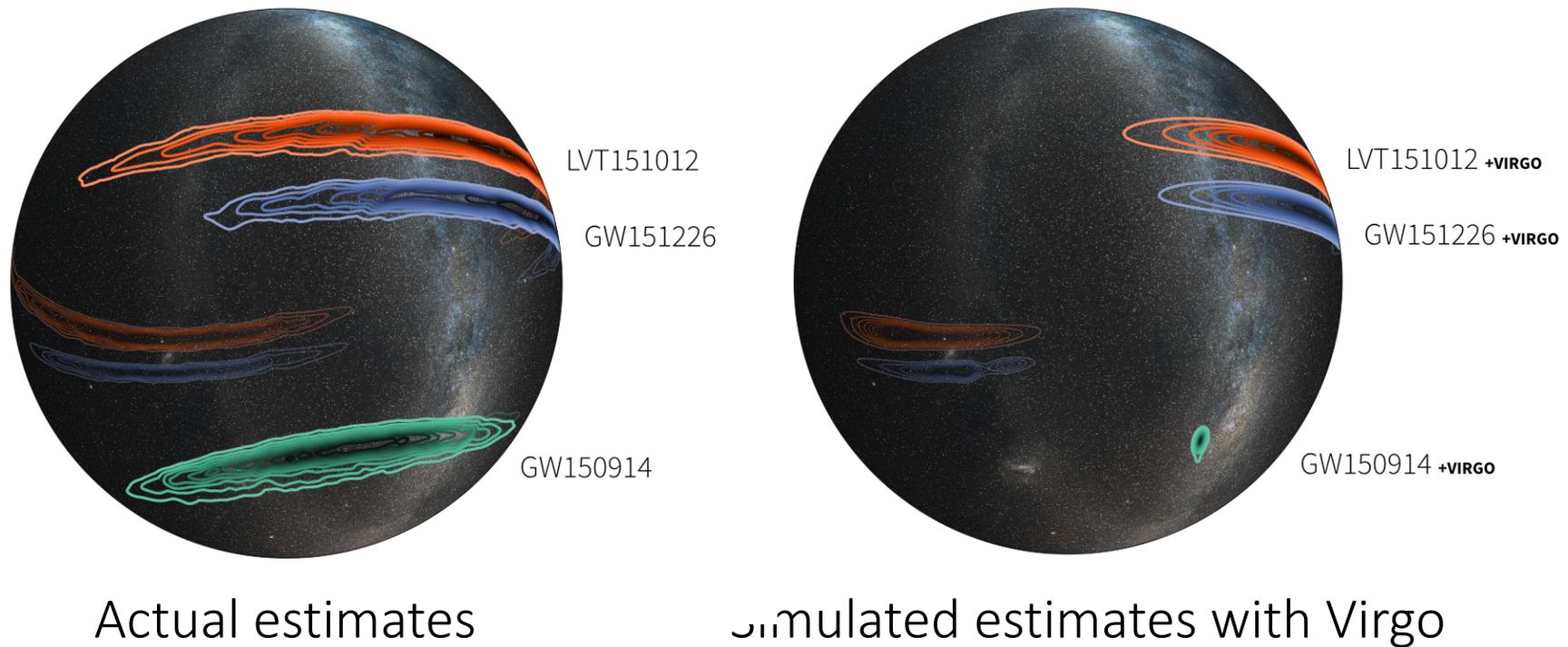


localization



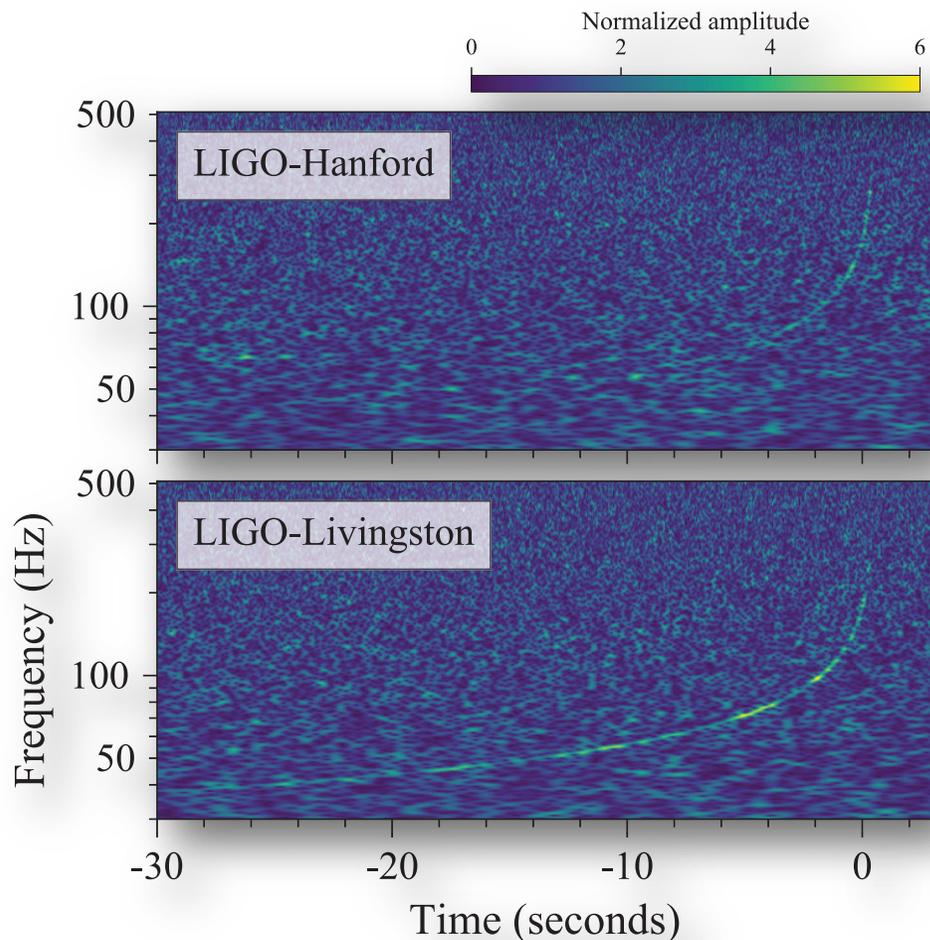
- 100-1000 deg²
- Improves with more detectors
- Difficult to cover for many optical observatories
- Significant transient foreground (SNe)
- 1/month FAR LIGO triggers

MORE DETECTORS NEEDED

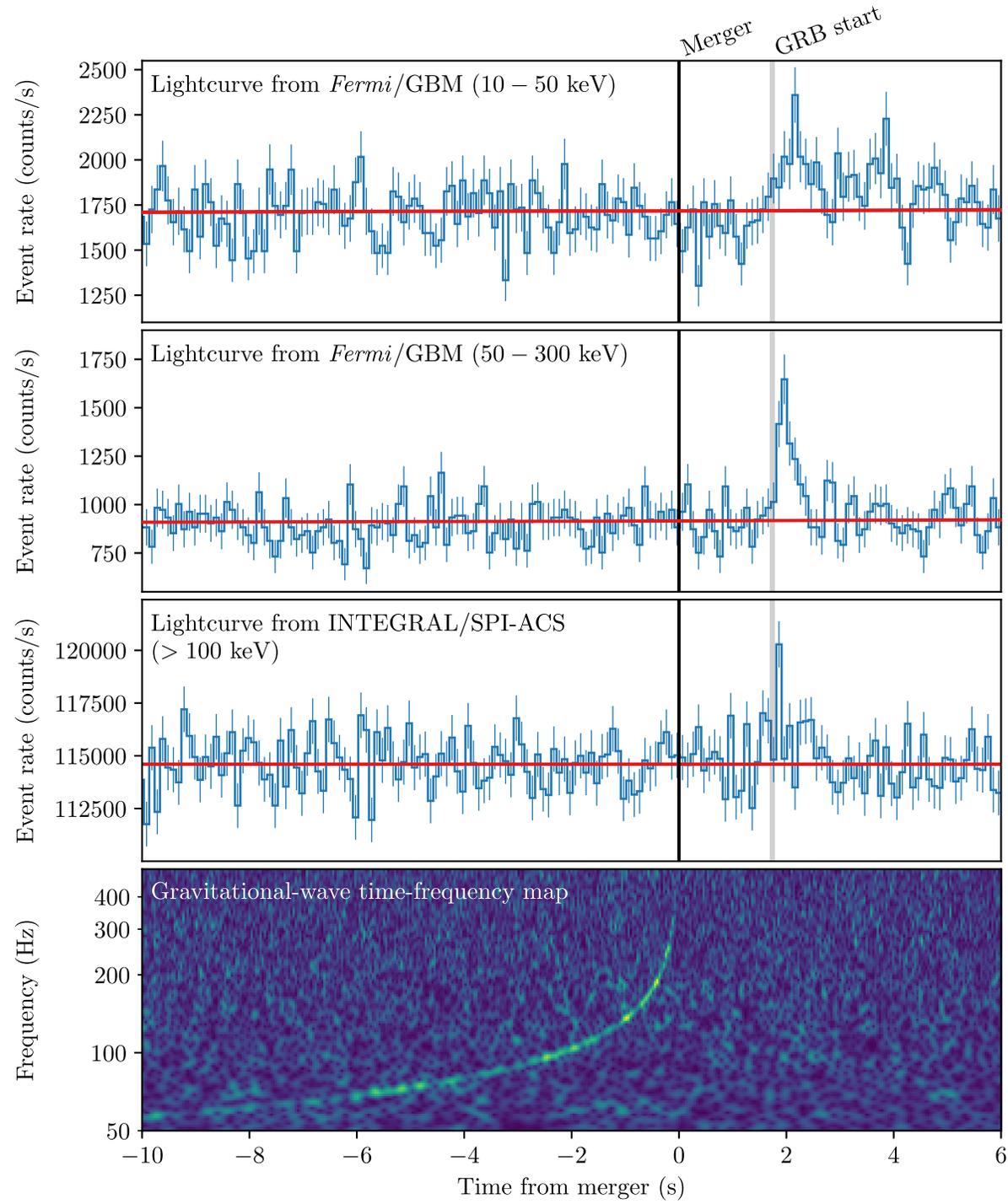


3-D projection of the Milky Way onto a transparent globe shows the probable locations of confirmed detections GW150914 (green), and GW151226 (blue), and the candidate LVT151012 (red). The outer contour for each represents the 90 percent confidence region while the innermost contour is the 10 percent region. Image credit: LIGO/Axel Mellinger.

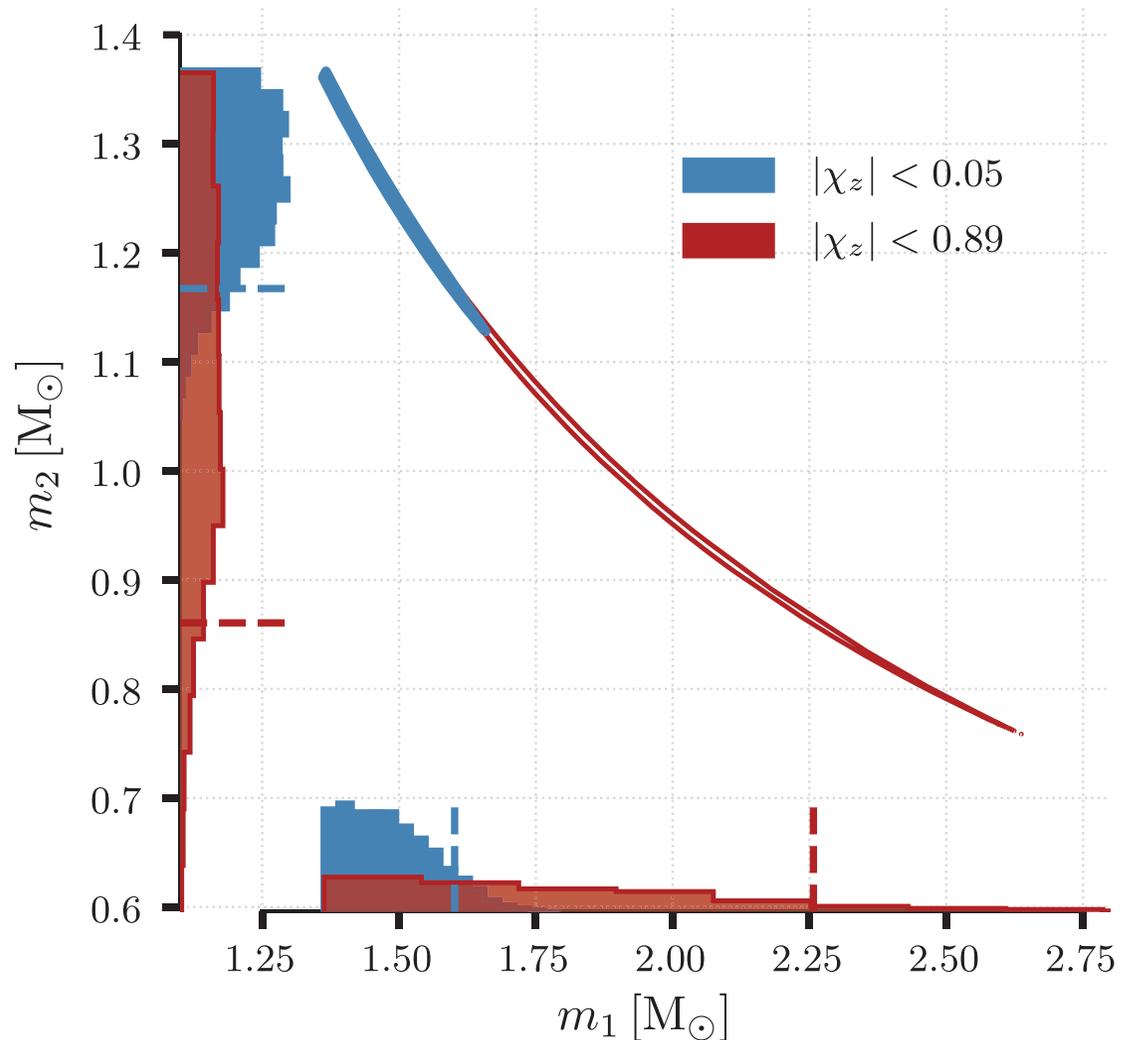
August 17, 2017



- Gravitational-wave trigger in LIGO-Hanford only
- Livingston – noise transient
- No signal in Virgo
- Consistent with BNS merger
- 1.7s later --- GRB alert from Fermi
- Weak GRB ($\sim 10^{-7}$ erg cm $^{-2}$)



Information in Gravitational Waves



| Low-spin priors ($ \chi \leq 0.05$) | |
|--|-----------------------------------|
| Primary mass m_1 | $1.36\text{--}1.60 M_\odot$ |
| Secondary mass m_2 | $1.17\text{--}1.36 M_\odot$ |
| Chirp mass \mathcal{M} | $1.188^{+0.004}_{-0.002} M_\odot$ |
| Mass ratio m_2/m_1 | $0.7\text{--}1.0$ |
| Total mass m_{tot} | $2.74^{+0.04}_{-0.01} M_\odot$ |
| Radiated energy E_{rad} | $> 0.025 M_\odot c^2$ |
| Luminosity distance D_L | $40^{+8}_{-14} \text{ Mpc}$ |
| Viewing angle Θ | $\leq 55^\circ$ |
| Using NGC 4993 location | $\leq 28^\circ$ |

$$R = 1540^{+3200}_{-1220} \text{ Gpc}^{-3} \text{ yr}^{-1}$$

- More common than we expected
- Consistent with galactic BNS observations
- Tidal effects are not taken into account
- Neutron star maximum mass: $\sim 2.2 M_{\text{sun}}$

Constraints on Cosmology with Gravitational Waves

- Uncertainty:
 - Inclination
 - Peculiar velocity of host galaxy
 - Natal kick
- More and more distant detections will significantly shrink this uncertainty

