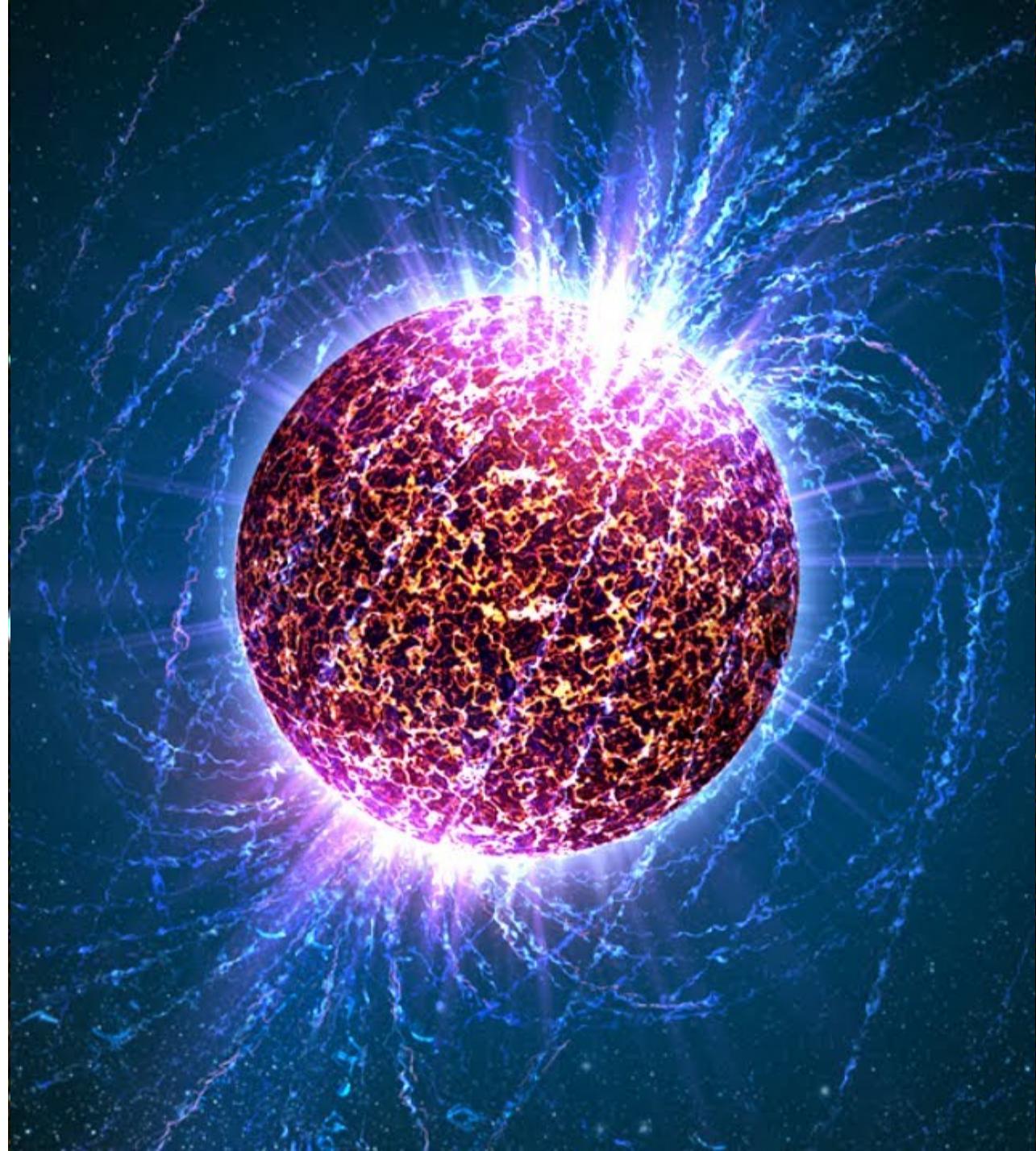


Lecture VIII.

Neutron stars



Imre Bartos | Fall 2018



Homework

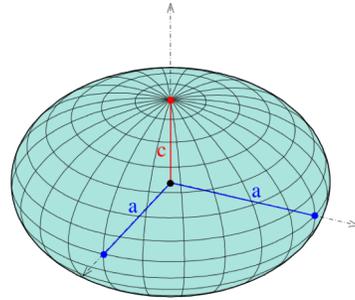
$$E_{\text{GW}} \approx 10^{-2} M_{\odot} c^2 \left(\frac{\epsilon}{0.2} \right)^2 \left(\frac{f}{2 \text{ kHz}} \right)^6 \left(\frac{M}{1.4 M_{\odot}} \right) \left(\frac{R}{12 \text{ km}} \right)^2 \left(\frac{\tau}{0.1 \text{ s}} \right)$$

Assume realistic dependence of epsilon on f.

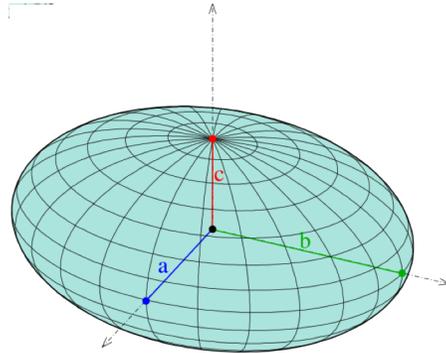
What will be the gravitational waveform?

Rotating Spheroids

MacLaurin spheroids



Jacobi spheroids
(or Dedekind spheroids)



Dynamically unstable:

- $T/|W| > 2.7$
- $e > 0.95$ (1:3:3)



Secular instability:

- $T/|W| > 1.4$
- $e > 0.81$ (1:1.7)

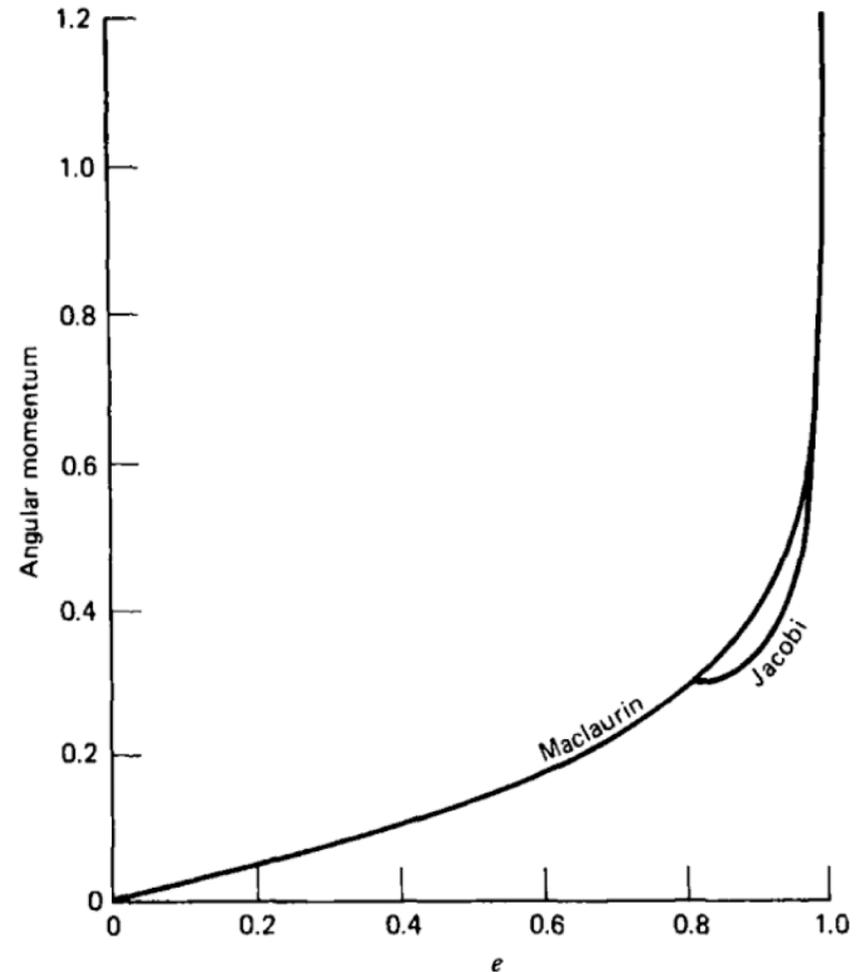


Figure 7.3 The angular momentum [in the unit $(GM^3\bar{a})^{1/2}$] along the **Maclaurin** and the Jacobian sequences. Here \bar{a} is related to the three semimajor axes by $\bar{a} \equiv (abc)^{1/3}$; for a **Maclaurin** spheroid $a = b$. The abscissa in both cases is the eccentricity defined by Eq. (7.3.9). [Reproduced, with permission, from *Ellipsoidal Figures of Equilibrium* by S. Chandrasekhar, published by Yale University Press. © 1969 by Yale University.]

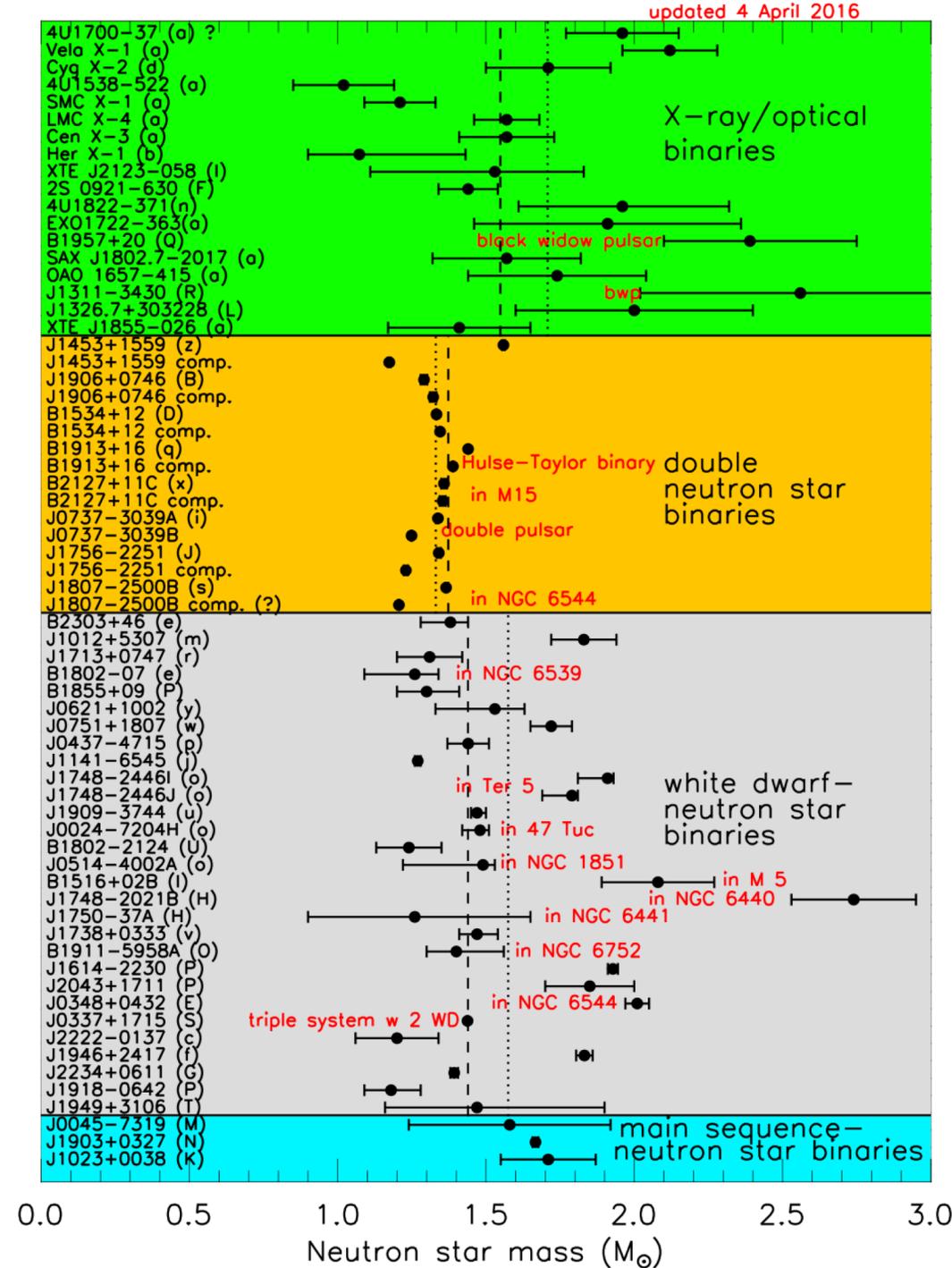
Properties - Mass

There should be a lower limit just from formation. --- 1.1 Msun

Maximum observed mass --- ~2 Msun

Maximum mass from GW170817 --- 2.17 Msun

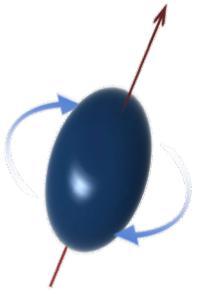
Mass distribution depends on NS companion



Magnetic field

Typically 10^4 - 10^{11} T

Newly born magnetars --- 10^{15} T

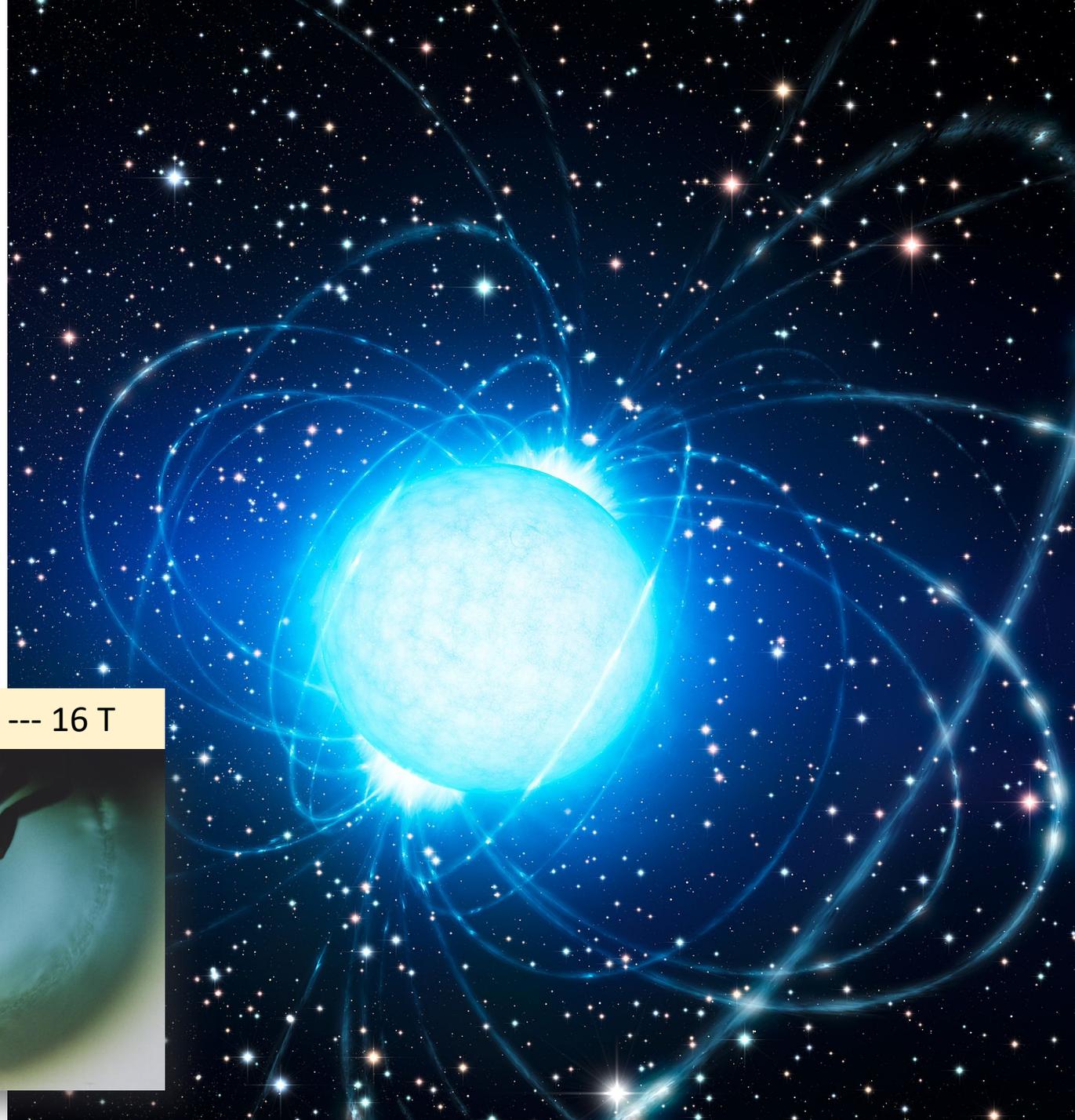


Can make NS prolate

After formation → dynamo effect
→ loss of angular momentum
↔ competing effect with GWs

NS slowly loses magnetic fields
→ weak during BNS merger

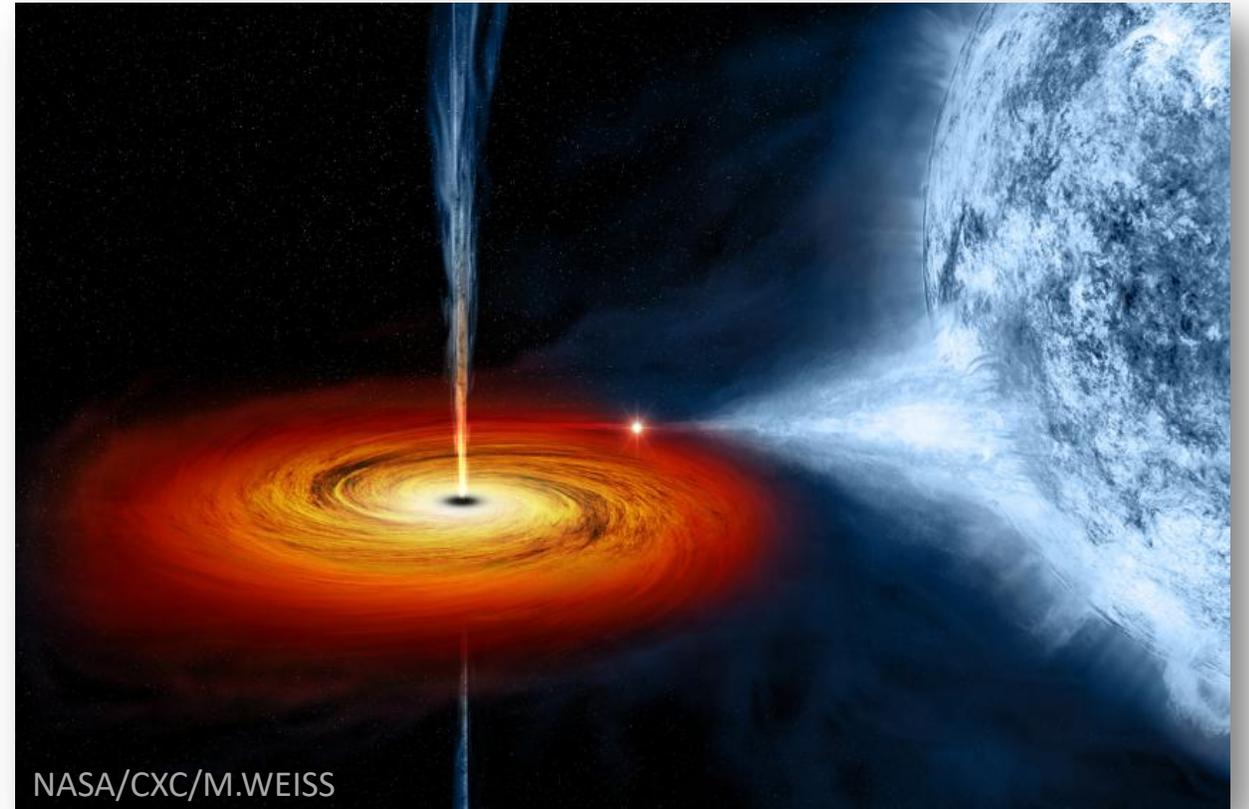
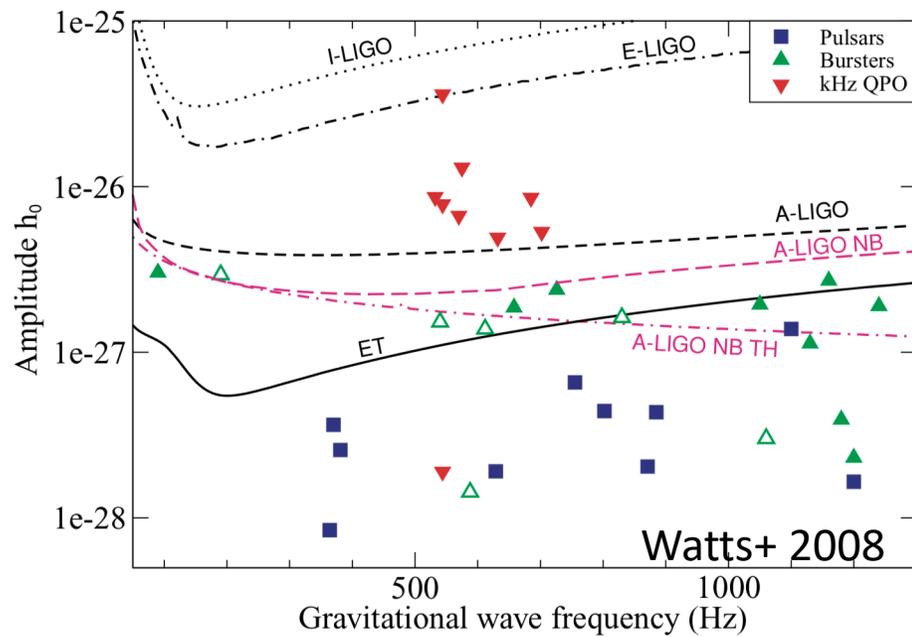
Frog levitation --- 16 T



Accretion and spindown

Many accreting NSs rotate around 300 Hz

Maybe GW emission?



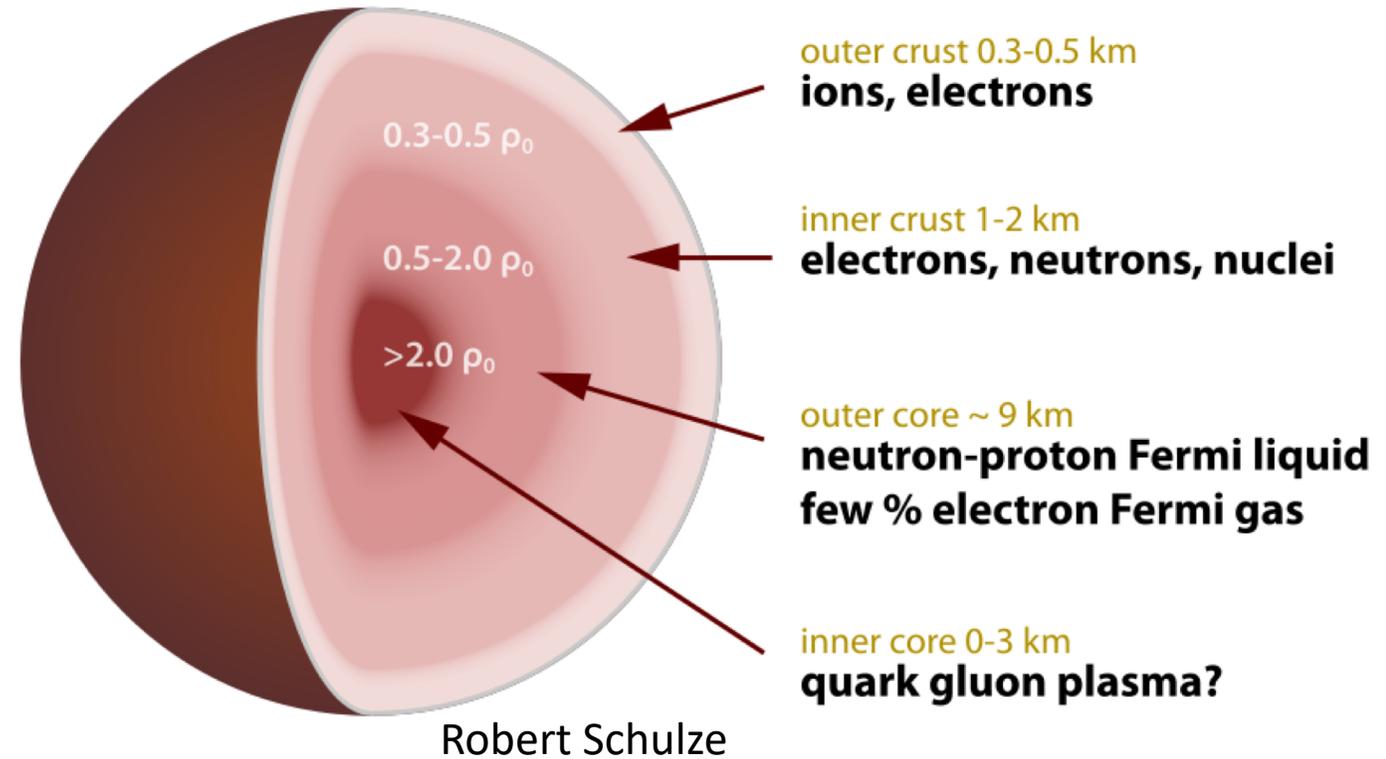
Structure

Mostly unknown

There is likely a NS “crust”

There is likely a NS “crust” and core

Quark-gluon plasma in core?



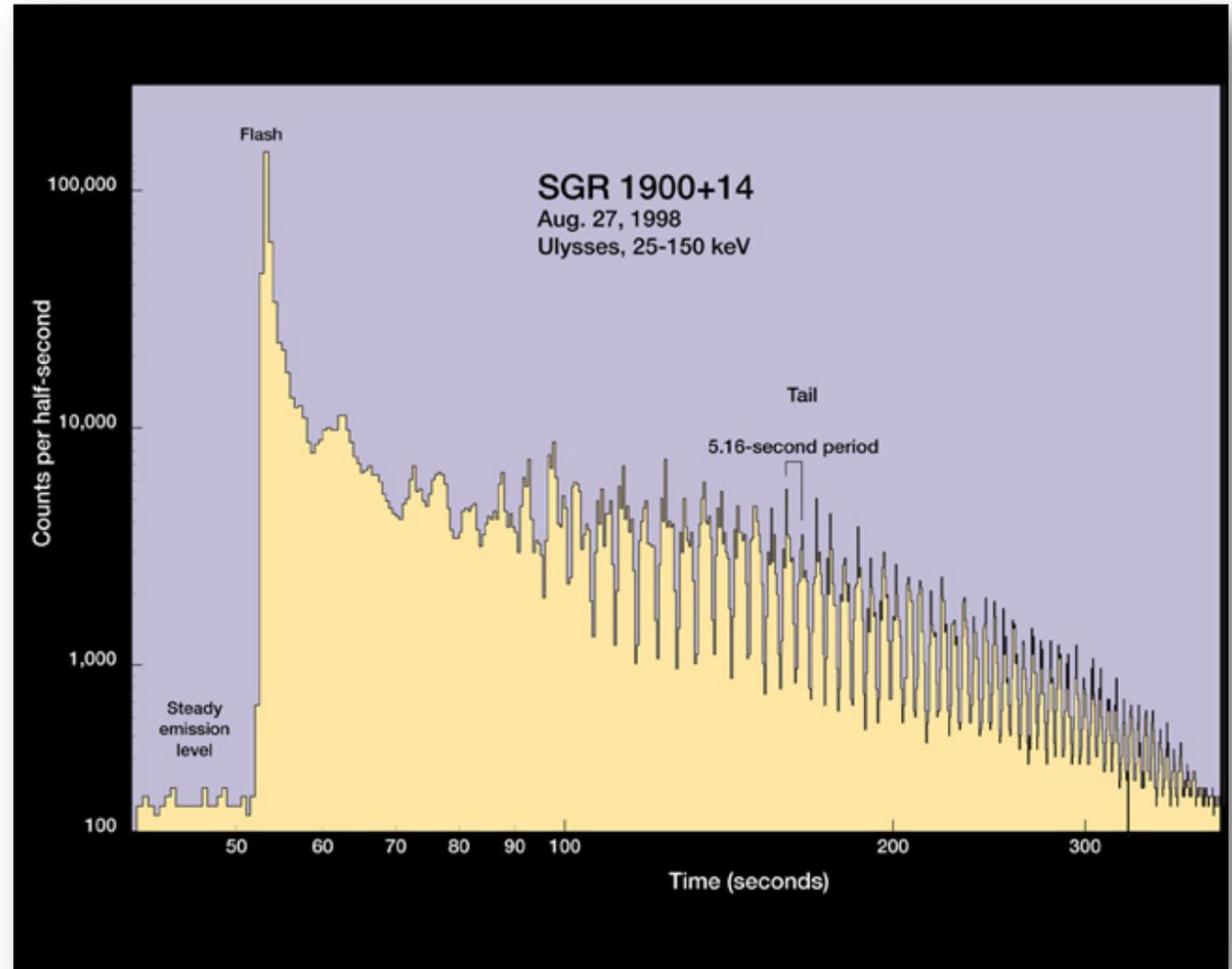
Soft gamma repeaters

Occasional outbursts of gamma rays

Quasi-periodic oscillations

Starquakes??

Magnetic field reorganization?



Glitches

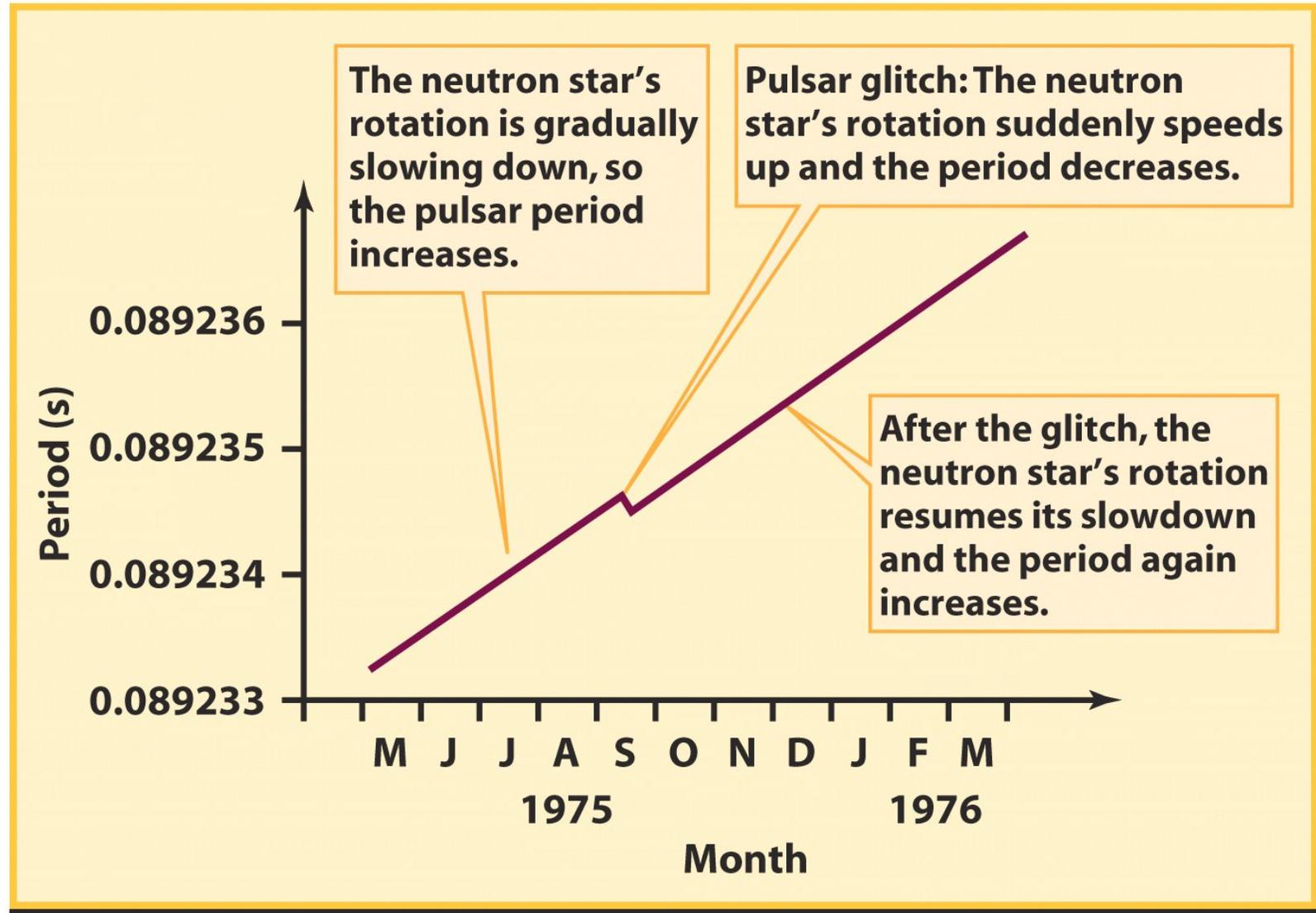
Starquakes?

NS crust ruptures
→ radius decreases
→ faster rotation

Core reorganization that
releases energy?

Anti-glitches
Unclear??

Bad for pulsar timing



Pulsars

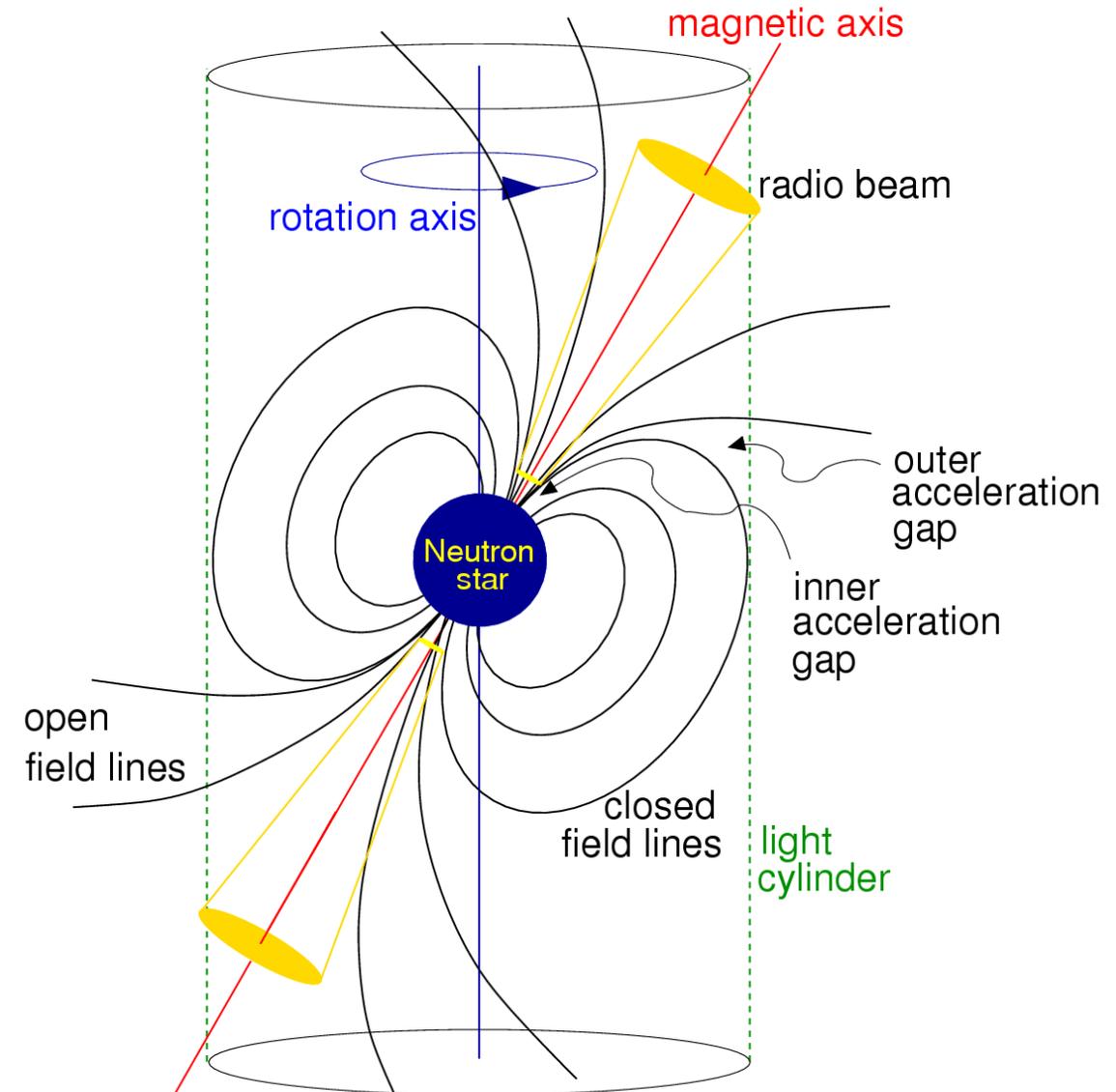
Very regular period

Formed in a supernova

After sufficient slowdown the radio pulsar mechanism is turned off.

Energy source:

- Rotation
- Accretion
- Magnetic fields

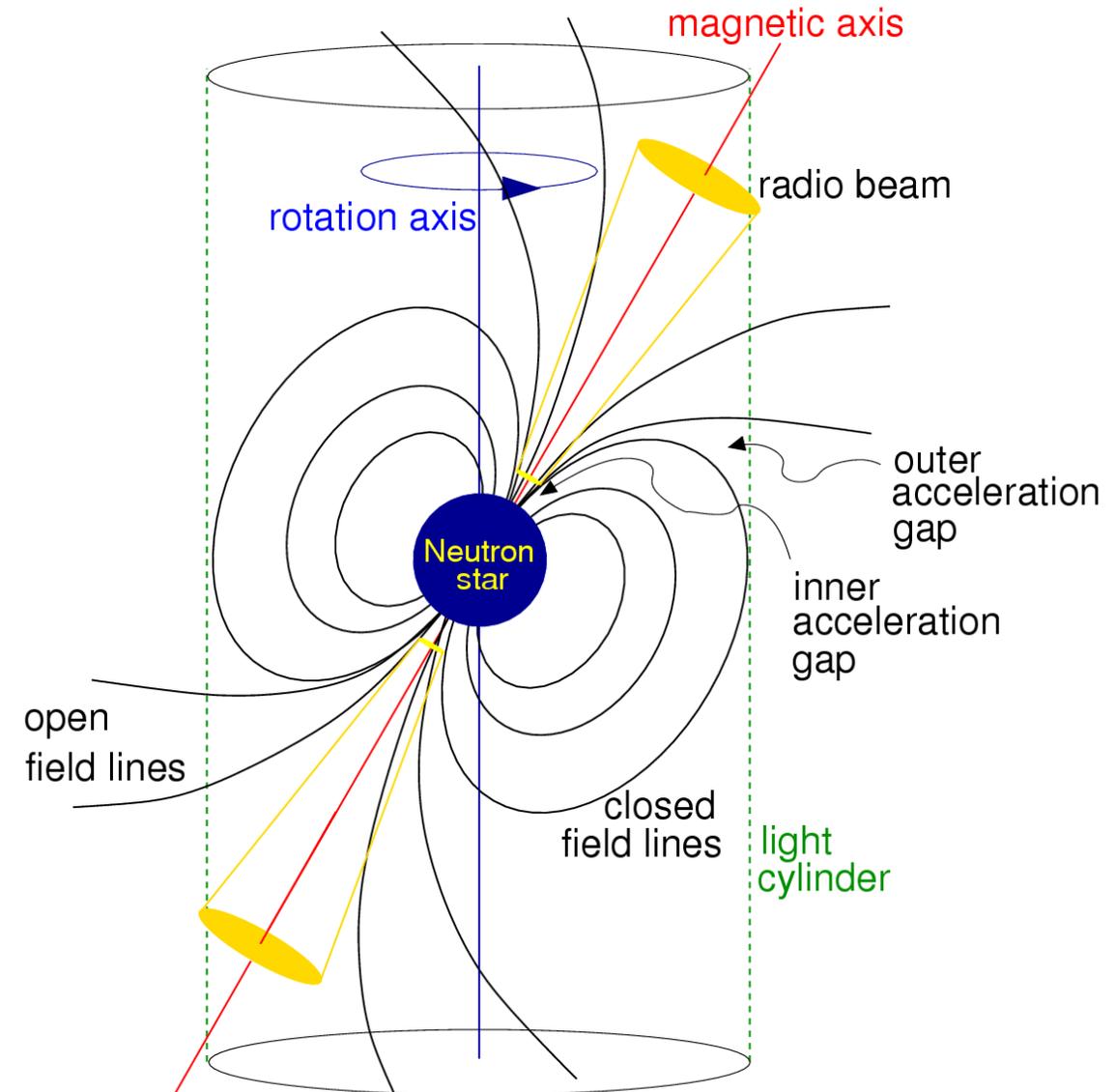


Pulsars

If the magnetic dipole is inclined from the rotation axis
→ Magnetic dipole radiation

We can find the magnetic field strength of the
NS from the spindown rate.

$$\left(\frac{B}{\text{Gauss}} \right) > 3.2 \times 10^{19} \left(\frac{P\dot{P}}{\text{s}} \right)^{1/2}$$



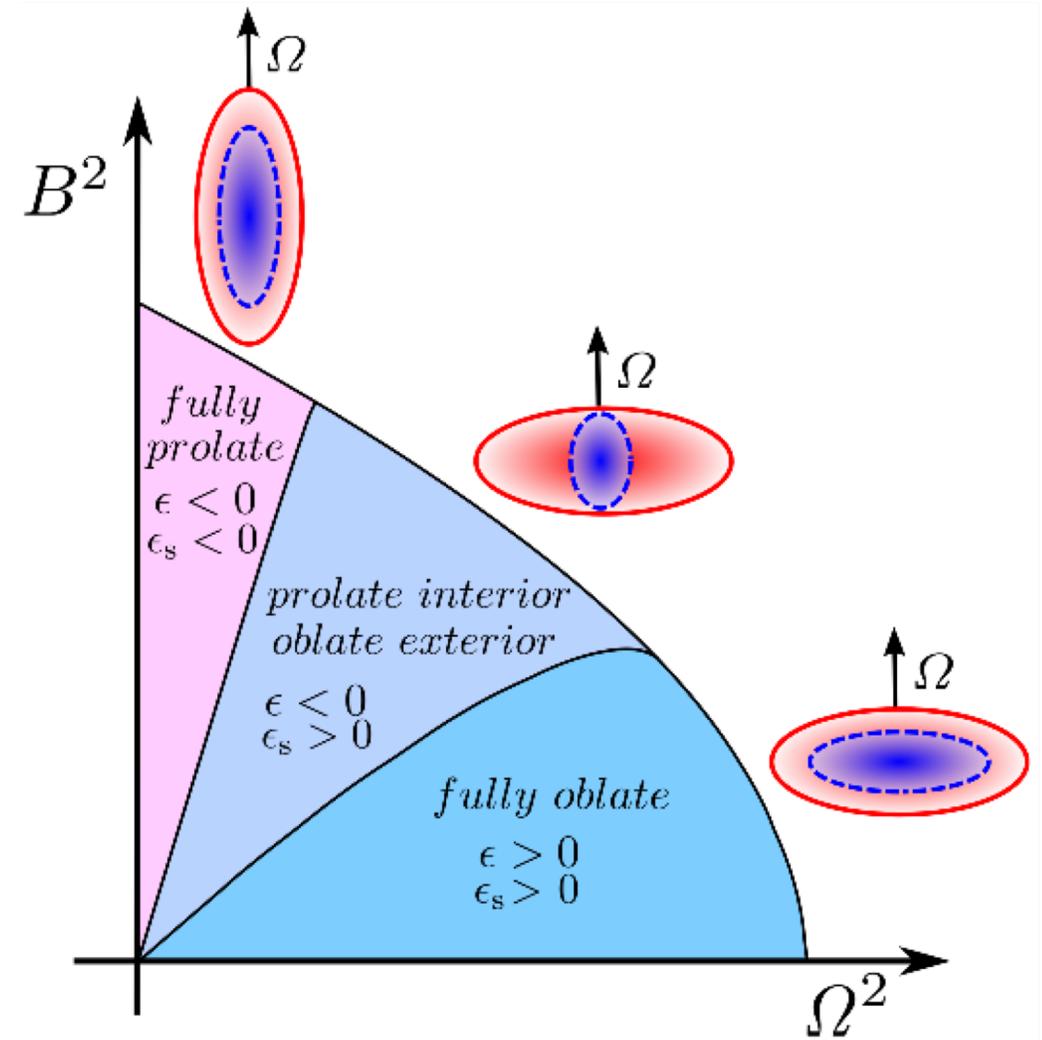
Magnetic deformation

If the magnetic dipole is inclined from the rotation axis
→ Magnetic dipole radiation

We can find the magnetic field strength of the NS from the spindown rate.

$$\begin{aligned}\epsilon &= -\frac{3}{2}\epsilon = \frac{1}{18} \frac{B^2 R^4}{GM^2} \\ &\approx 10^{-12} \left(\frac{R}{10\text{ km}}\right)^4 \left(\frac{M}{1.4 M_\odot}\right)^{-2} \left(\frac{\bar{B}}{10^{12}\text{ G}}\right)^2\end{aligned}$$

Haskell+ 2002



Fieben & Rezzolla 2014

Spin Down

Longer period typically means higher spindown rate.

If luminosity \sim spin down power
 \rightarrow rotation powered

Spindown rate and period gives us an estimate on the characteristic age of the pulsar.

