

Homework A

PHY3513

Due: Wednesday, Jan 22

1. (a) $2 + \frac{1}{2} + \frac{1}{3!} + \frac{1}{4!} + \frac{1}{5!} + \dots = ??$

(b) $1 - \frac{1}{2} + \frac{1}{3} - \frac{1}{4} + \frac{1}{5} - \frac{1}{6} + \dots = ??$

2. Expand $(1 - 2tz + t^2)^{-1/2}$ in powers of t assuming that t is small. Collect the coefficients of t^0 , t^1 , and t^2 .

3. The displacement z of a particle of rest mass m_0 , resulting from a constant force m_0g along the z -axis is

$$z = \frac{c^2}{g} \left\{ \left[1 + \left(g \frac{t}{c} \right)^2 \right]^{1/2} - 1 \right\}$$

including relativistic effect. Find the displacement z as a power series in time t . Compare with the classical result,

$$z = \frac{1}{2} g t^2.$$

4. A magnetic system has specific heat which is a function of applied magnetic field, H and temperature, T . It can be represented theoretically by

$$C(T, H) = C(H/T) = N \frac{(H/T)^2}{\cosh^2(H/T)}$$

where N is constant.

(a) Expand $C(T, H)$ in power of (H/T) up to $(H/T)^4$ assuming $H \ll T$.

(b) Sketch (freehand) the behavior of your answer as a function of $x = H/T$.

5. (1.4) For parts (a) and (b) express answers as whole numbers to a precision of ± 1 , for (c) use Stirling's formula and express answer as 10 raised to some power.

6. The probability $P(n)$ that an event characterized by a probability p occurs n times in N trials is given by the binomial distribution

$$P(n) = \frac{N!}{n!(N-n)!} p^n (1-p)^{N-n}.$$

Consider a case where $p \ll 1$ and $N \gg 1$.

(a) Show that $(1 - p)^{N-n} \approx e^{-Np}$ using $\ln(1-p) \approx -p$.

(b) Show that $N!/(N-n)! \approx N^n$.

(c) Therefore, you can show that $P(n) = \frac{\lambda^n}{n!} e^{-\lambda}$ where $\lambda = Np$. You have just demonstrated that the binomial distribution for small p and large N turns into the Poisson distribution!

7. (2.5)

8. (3.3)

9. (3.4)

10. (3.5) Do (a) through (g), skip (h) and (i), and do (j).