

-- Force:  $\leftrightarrow$  interaction

\* units of force - N (newton) =  $1 \text{ kg} \cdot \text{m} / \text{s}^2$

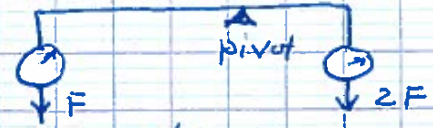
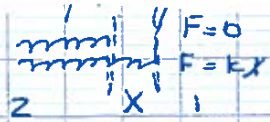
\* How to measure: Spring

Hooke's Law:  $F = kx$

Force field (vector field)

spring balance

by adjusting the pivot we can calibrate it.



-- Mass - measure of the object's inertia - its resistance to being accelerated.

What is the origin of mass? CM is not concerned with this philosophical question.

\* inertial balance - a way how we can compare masses

\* Units of mass: just pick some reference mass and call it a kilogram. All other masses are measured in units of the ref. mass.

\* mass  $\neq$  weight - what is the difference? "inertia"  $\leftrightarrow$  "force" due to Earth gravity.

\* Inertial mass vs gravitational mass

1) no measurable difference

2)  $IM \equiv GM$  - the equivalence principle.

-- Newton's First & Second Laws

\* the law of inertia (see the book)

\*  $\vec{F} = m\vec{a}$   $\vec{a} = \vec{F}/m$   $\vec{F}$  is the sum of all forces acting on the particle.

$m\vec{\ddot{r}} = \vec{F}$   
diff. equation  
(chapter 1.4)

$\vec{F} = m\vec{a} = m\dot{\vec{v}} = \dot{\vec{p}}$  - rate of change of the particle momentum  
momentum:  $\vec{p} = m\vec{v}$

\* Reference frames (chapter 1.4)

the role of the first law  $\rightarrow$  distinguish between "inertial" and "non-inertial" frames

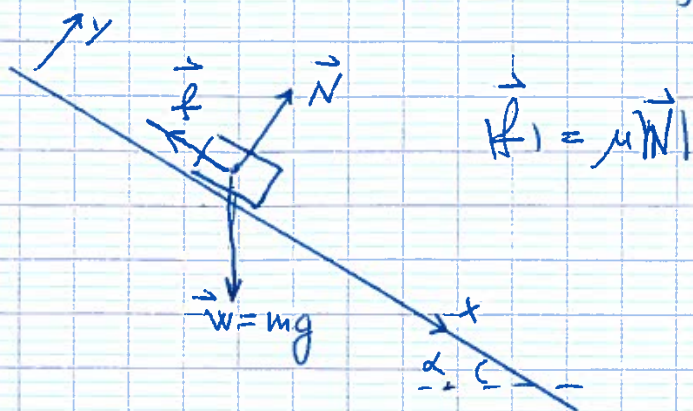
Validity of  $N1$  &  $N2$  Laws  
(chapter 1.4)

FIGURE 1.4 from the book.

The laws of nature do not depend on selection of the ref. frame, but our formulation of laws of nature do

L3

Example 1.1 a block sliding down an incl  
(for details see the text book)



$$a) \quad \dot{y} = 0 \rightarrow F_y = 0 = N - mg \cos \alpha = 0$$

$$N = mg \cos \alpha$$

$$b) \quad f = \mu N = \mu mg \cos \alpha$$

$$c) \quad F_x = mg \sin \alpha - f = mg (\sin \alpha - \mu \cos \alpha) = \ddot{x}$$

$$\ddot{x} = g (\sin \alpha - \mu \cos \alpha) \quad \text{- diff. eq. for}$$

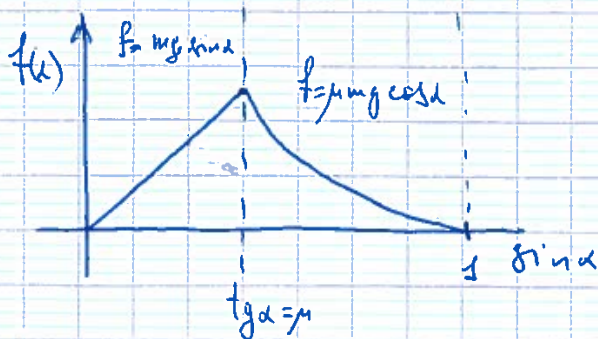
$$\ddot{x} = \text{const. !}$$

$$\dot{x} = g (\sin \alpha - \mu \cos \alpha) t + v_0 = 0 \quad \text{at } t=0$$

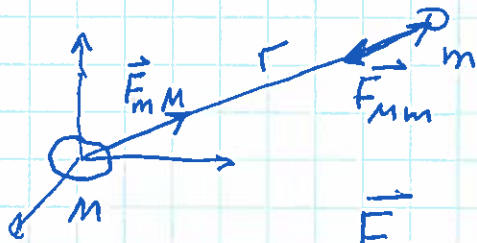
$$x = \frac{1}{2} g t^2 (\sin \alpha - \mu \cos \alpha) + x_0 = 0 \quad \text{at } t=0$$

Caveat: What if  $\sin \alpha - \mu \cos \alpha < 0$ ?

$$f(\alpha) \leq \mu N$$



\* Newton's law of gravitation



$$\vec{F}_{mM} = -\frac{GMm}{r^2} \hat{r} \quad \text{— force from } M \text{ to } m$$

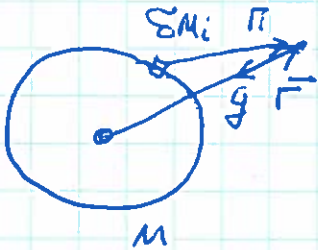
$$\vec{F}_{Mm} = \frac{GMm}{r^2} \hat{r} \quad \text{— force from } m \text{ to } M$$

\* gravitational field (acceleration)

$$\vec{g}_M = \vec{F}_{mM}/m = -\frac{GM}{r^2} \hat{r}$$

$$\vec{g}_m = \vec{F}_{mM}/M = \frac{GM}{r^2} \hat{r}$$

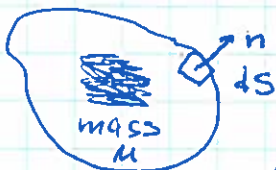
\* gravitational field of a sphere of mass M



$$\delta g_i = -\frac{G\delta M_i}{r_i^2} \hat{r}_i$$

$$\vec{g} = -\sum_i \frac{G\delta M_i}{r_i^2} \hat{r}_i = -\frac{GM}{r^2} \hat{r}$$

\* Gauss flux theorem for gravity



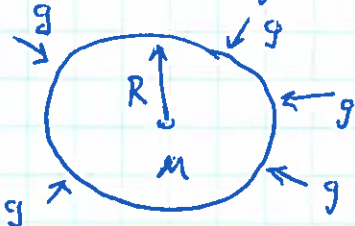
Surface S

$$\oint \vec{g} \cdot d\vec{S} = -4\pi GM$$

↑ surface integral

$d\vec{S}$  - vector along the direction of the surface normal  $\hat{n}$  ( $d\vec{S} = |dS|\hat{n}$ ) with magnitude  $|dS|$

\* gravity of Earth (assuming solid <sup>uniform</sup> sphere)



$$\oint \vec{g} \cdot d\vec{S} = 4\pi R^2 g = -4\pi GM$$

$$g = -\frac{GM}{R^2}$$